UHECRs and the Galactic magnetic field

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Two outstanding questions:

Is astronomy with UHECRs possible?

- protons vs nuclei as primaries
- role of magnetic fields

• Is physics beyond the SM needed to explain UHECR events?

- energy spectrum consistent with GZK suppression?
 - suppression depends on number of sources, their minimal distances, magnetic fields, ...
- correlations with sources at cosmological distances?

Cosmic ray spectrum: the dip at $10^{19}~{ m eV}~{ m [Berezinsky, Grigorieva, Hnatyk '04]}$



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Transition to extragalactic protons



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Transition to extragalactic protons



dip suggests: primaries above 10^{18} eV are extragalactic protons

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Chemical composition studies-photon limits



Chemical composition studies-photon limits



protons or nuclei are main primaries

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Chemical composition studies



Chemical composition studies



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Small-scale clusters and density of sources:



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Extragalactic magnetic field – simulation by SME:





Extragalactic magnetic field – simulation DGST:



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Extragalactic magnetic field – simulation DGST:



DGST: astronomy with UHE protons possible in large part of sky!

which simulation/conclusion is closer to reality?

- many technical differences between the two simulations; two major conceptional ones:
 - Sigl, Miniato, Ensslin use an unconstrained simulation, putting observer * close to a cluster



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- Dolag, Grasso, Springel, Tkachev inject protons uniformly on a sphere
- Sigl, Miniato, Ensslin inject protons following matter distribution

Models Deflections (De-) Magnification

Modelling the regular Galactic field:

• thin disc field ressembles matter structure

$$B(\rho, \vartheta) = b(\rho) \cos\left(\vartheta - \frac{1}{\tan p} \ln(\rho/\xi_0)\right)$$



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- only torodial component
- (anti-) symmetric for $\vartheta \rightarrow \vartheta + \pi$: BSS or ASS

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- (anti-) symmetric for $\vartheta \to \vartheta + \pi :$ BSS or ASS
- vertical profile more uncertain:
 - (anti-) symmetric for $z \rightarrow -z$: A or S

$$B(\rho,\vartheta,z) = \frac{f(z)B(\rho,\vartheta)}{f(z)B(\rho,\vartheta)}$$

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vertical profile more uncertain:

• (anti-) symmetric for $z \rightarrow -z$: A or S

$$B(\rho,\vartheta,z) = f(z)B(\rho,\vartheta)$$

• even more uncertain: halo or dipole component

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Models Deflections (De-) Magnification

GMF Models considered:

• Tinyakov & Tkachev (TT):

- BSS-A
- $f(z) = \operatorname{sign}(z) \exp(-|z|/z_0)$ and $z_0 = 1.5$ kpc

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- Harari, Mollerach & Estaban (HMR):
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- Prouza & Smida (PS):
 - BSS-S
 - $f(z) = \exp(-|z|/z_0)$ with $z_0 = 0.2$ kpc
 - toroidal thick disc/halo contribution with width 0.3 kpc
 - dipole field

Models Deflections (De-) Magnification

Effects of the GMF:

• arrival directions at entrance in Galaxy should be used in (auto-) correlation studies

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Models Deflections (De-) Magnification

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- (de-) magnification in GMF changes effective exposure:

 $\boldsymbol{\omega}(b,l) = \boldsymbol{\omega}_{\exp}(b,l)\boldsymbol{\omega}_{\max}(b,l)$

 $\omega_{\rm mag}(b,l) = d\Omega_{\oplus}/d\Omega_{\infty}$

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- should be included in estimates of stat. significance of (auto-) correlations
- technical complications: energy dependence of ω, singular points and lines, backtracing

Models Deflections (De-) Magnification

Comment on Liouville theorem:

- isotropic flux outside GMF remains isotropic
- GMF does not create, only enhances anisotropies

Models Deflections (De-) Magnification

Comment on Liouville theorem:

- isotropic flux outside GMF remains isotropic
- GMF does not create, only enhances anisotropies
- but distribution of "effective" sources is anisotropic or $\omega_{mag} \neq 1$



Models Deflections (De-) Magnification

Deflections for $eE/Q = 10^{20}$ eV: TT model



Models Deflections (De-) Magnification

Deflections for $eE/Q = 10^{20} \text{eV}$: TT model

deflections $\gtrsim\!2.5^\circ$ at $4\!\times\!10^{19}$ eV in large fraction of sky



Models Deflections (De-) Magnification

Deflections for $eE/Q = 10^{20}$ eV: HMR model



Models Deflections (De-) Magnification

Deflections for $eE/Q = 10^{20} \text{eV}$: PS model



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Models Deflections (De-) Magnification

Comparison of models



Models Deflections (De-) Magnification

(De-) Magnification for $eE/Q = 4 \times 10^{19}$ eV: TT model



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Models Deflections (De-) Magnification

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Models Deflections (De-) Magnification

(De-) Magnification for $eE/Q = 4 \times 10^{19} \text{eV}$: HMR model



Models Deflections (De-) Magnification

(De-) Magnification for $E/Q = 2 \times 10^{19} \text{eV}$: HMR model



Models Deflections (De-) Magnification

Autocorrelation – without GMF correction:

[Tinyakov, Tkachev '01]



Models Deflections (De-) Magnification

Autocorrelation – with GMF correction:

hypothesis: proton primaries, weak EGMF and correct GMF model

- if correct, then w₁ should increase
- P_{\min} using $\omega_{GMF} = 1$ should decrease
- but P_{\min} with $\omega_{GMF} \neq 1$ should stay constant

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Autocorrelation – with GMF correction:

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- if correct, then w_1 should increase
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Model	w_1	$P(w > w_1)[\%]$	$P(w > w_1)$ for $\omega_{\text{GMF}} = 1$ [%]
-	11	1.1	1.1
TT	11	1.1	1.1
PS	10	5.0	2.9
HRM	9	8.7	5.7
HRM2	6	63	35

Summary

- deflections $> 2.5^\circ$ at 4×10^{19} eV in large fraction of sky
- deflections very model-dependent
- \Rightarrow makes correlation analysis more dubious
 - magnification in GMF might enhance small-scale clusters

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HMR model:

- BSS-S model with cosh profiles for both the disk and the halo field (⇒ spiral-like geometrical pattern for halo field)
- with scale heights respectively of $z_1 = 0.3$ kpc and $z_2 = 4$ kpc $f(z) = \frac{1}{2\cosh(z/z_1)} + \frac{1}{2\cosh(z/z_2)}$.
- $b(r) = \frac{3R_0}{r} \tanh^3(r/r_1)\mu$ G, with $r_1 = 2$ kpc, thus reducing to $b(r) \propto r^{-1}$ for $r > r_1$, while vanishing at the galactic center.
- pitch angle $p = -10^{\circ}$, and $\xi_0 = 10.55$ kpc.

 \Rightarrow

TT model:

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- $b(r) \propto r^{-1}$ for $r > r_{\min} \equiv 4$ kpc, and constant for $r \le r_{\min}$
- local field intensity of 1.4 μ G, pitch angle $p = -8^{\circ}$ and the parameter d fixed to -0.5 kpc.
- BSS-A with $f(z) = \operatorname{sign}(z) \exp(-z/z_0)$ with scale $z_0=1.5$

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PS model:

• BSS-S configuration with $z_0 = 0.2$ kpc, $p = -8^{\circ}$, d = -0.5 kpc, normalized to local field to 2 μ G

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$$B_{Tx} = -B_T \operatorname{sign}(z) \cos \vartheta$$
 $B_{Ty} = B_T \operatorname{sign}(z) \sin \vartheta$

where

$$B_T = \frac{B_{T,\max}(r)}{1 + \left(\frac{|z| - h_T}{w_T}\right)^2}$$

 h_T =1.5 kpc and w_T =0.3 kpc.

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PS model:

o dipolar field:

$$B_x = -3\mu_G \cos\varphi \sin\varphi \sin\vartheta/r_{tot}^3$$
$$B_y = -3\mu_G \cos\varphi \sin\varphi \cos\vartheta/r_{tot}^3$$
$$B_z = \mu_G (1 - 3\cos^2\varphi)/r_{tot}^3$$

where $\mu_G = 123\mu \text{G kpc}^3$ is the magnetic moment of the Galactic dipole, assumed $B_z \simeq +0.2\mu \text{G}$ near the Solar System.

• replaced by a constant field $B_z = -1mG$ in a sphere of 500 pc around GC

 \Rightarrow