

300 лет
Российская Академия Наук

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(1908–1994)



XVI
Марковские чтения,
посвященные 115-летию
со дня рождения М.А. Маркова
17 мая 2023
Москва



Астрофизические проявления первичных черных дыр

Константин Постнов
ГАИШ МГУ

Plan

- Introduction
- PBH in LVK GWTC-3 data
- PBH as seeds of SMBH in early galaxies

PBH formation

Zeldovich, Novikov'67, Carr, Hawking'74....

M_h

$r_h = 2t$

$M_h = m_{pl}^2 t$

$\approx 2.2 \times 10^5 M_\odot \frac{t}{1s}$

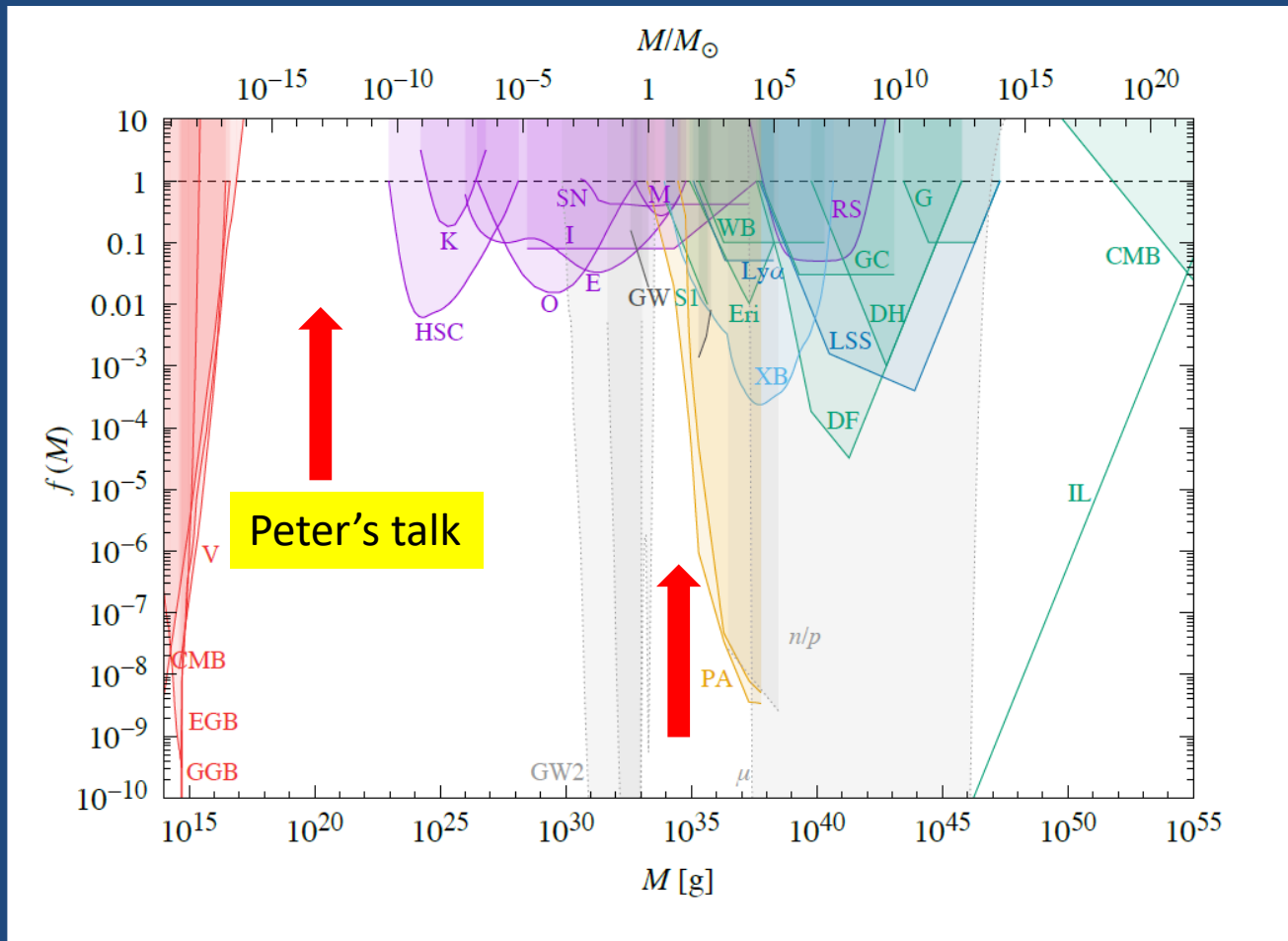
$\approx 8 M_\odot \left(\frac{100 \text{ MeV}}{T_{QCD}} \right)^2 \left(\frac{40}{g_*} \right)^{1/2}$

$R \leq \frac{2M}{m_{pl}^2}$

$\frac{\delta\rho}{\rho} \geq \left(\frac{M_h}{M} \right)^2$

Dolgov+KP 2004.1699

PBH constraints (model-dependent)



Some PBH formation scenarios

- Primordial density fluctuations, $\delta > \delta_c \sim 0.45$ (model-dependent)
- Collapse of scale-invariant fluctuations \rightarrow power-law mass spectra $dn/dM \sim M^{-\alpha}$, $\alpha = 2(1+2w)/(1+w) = 2.5$ at RD ($w=1/3$)
- Inflationary models \rightarrow **log-normal mass spectrum**

$$\frac{dn}{dM} = \mu^2 \exp[-\gamma \ln^2(M/M_{max})] \quad (\text{Dolgov, Silk 1993})$$

- QCD phase transition at $T=100-200$ MeV:

$$M \sim \left(\frac{m_{pl}}{m_p}\right)^3 m_p \sim M_{ch} \approx 1 M_\odot$$

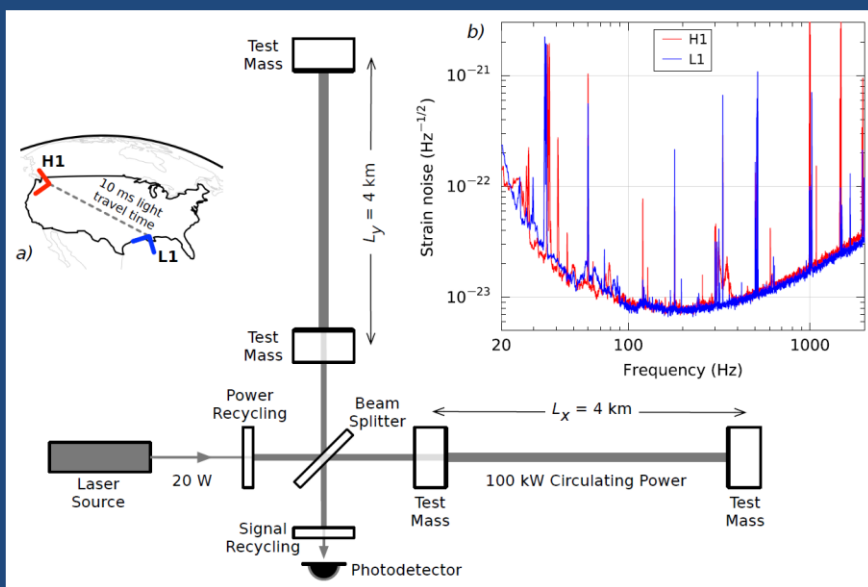
- Bubble collisions, cosmic strings ...

I. PBH in GW observations



Laser interferometers

LIGO 1990-2017 ~690 MUSD



19.05.2023

Марковские чтения 2023

LIGO
Hanford
USA



KAGRA
Kamioka
Japan



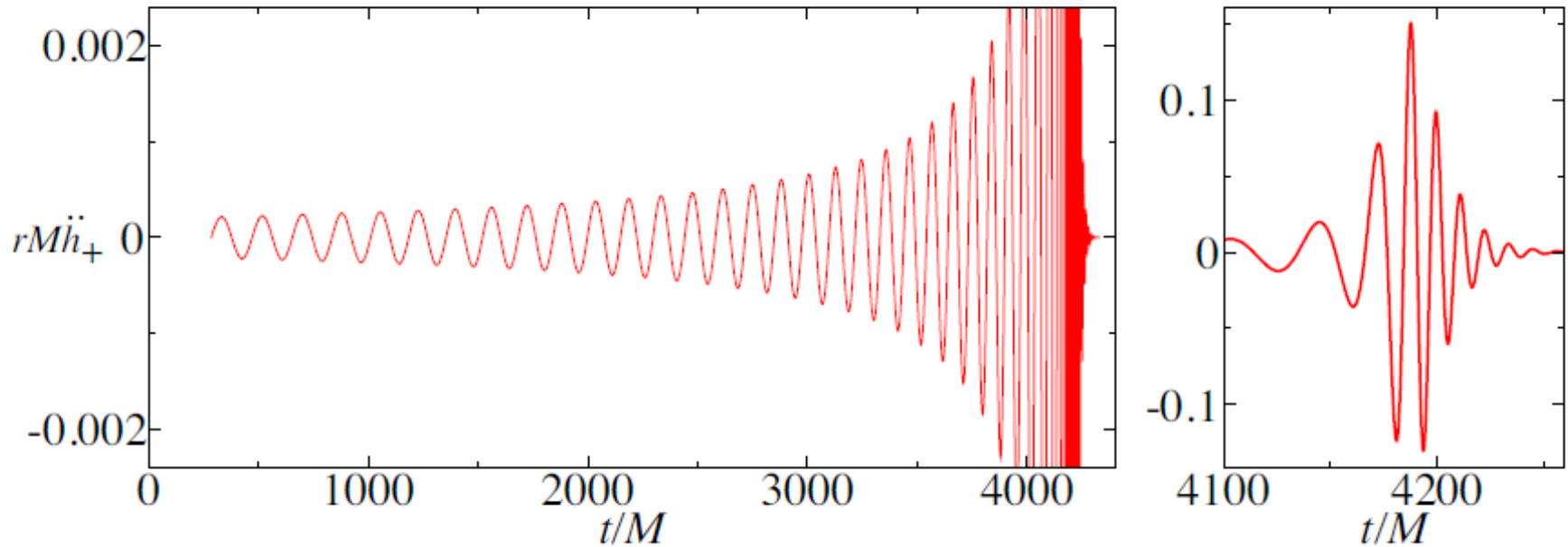
Virgo
Pisa
Italy



LIGO
Livingston
USA



Chirp signal from coalescing binary system



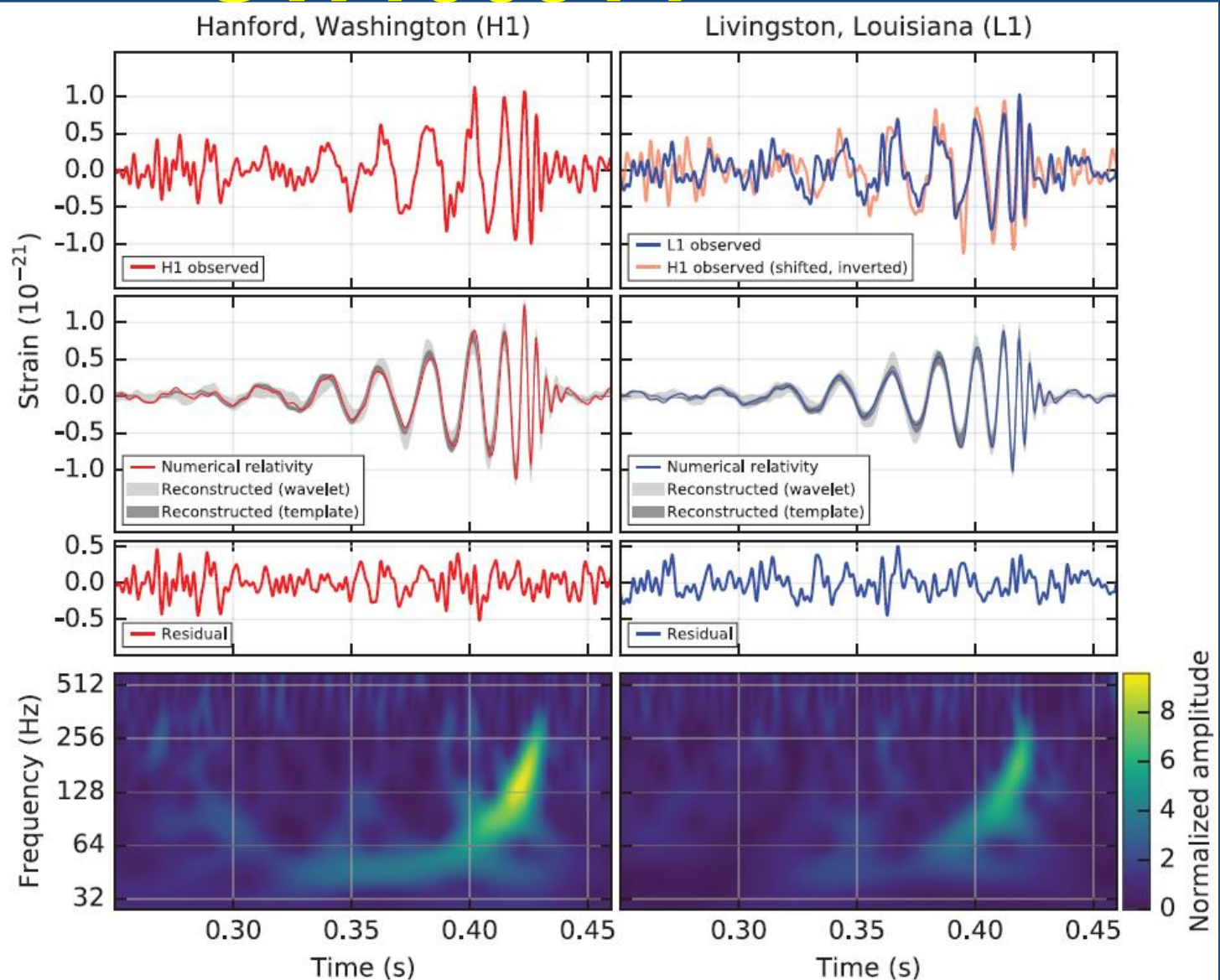
$$h_+ = h_{\hat{\theta}\hat{\theta}}^{\text{TT}} = \frac{2}{r} [\ddot{I}_{\hat{\theta}\hat{\theta}}(t-r)]^{\text{TT}} = -2(1 + \cos^2 \theta) \frac{\mu(M\Omega)^{2/3}}{r} \cos[2(\Omega t - \Omega r - \phi)]$$

$$h_\times = h_{\hat{\theta}\hat{\phi}}^{\text{TT}} = \frac{2}{r} [\ddot{I}_{\hat{\theta}\hat{\phi}}(t-r)]^{\text{TT}} = -4 \cos \theta \frac{\mu(M\Omega)^{2/3}}{r} \sin[2(\Omega t - \Omega r - \phi)] .$$

GW150914

PRL 116, 061102 (2016)

35-350 Hz bandpass filter applied



Chirp signal from inspiraling binaries

- Chirp-mass determined inspiraling signal

$$M_{ch} = (\mu^3 M^2)^{1/5}$$

$$h \sim M_{ch}^{5/3} f^{2/3} / r$$

$$\mathcal{M} = \frac{(m_1 m_2)^{3/5}}{(m_1 + m_2)^{1/5}} = \frac{c^3}{G} \left(\frac{5}{96} \pi^{-8/3} f^{-11/3} \dot{f} \right)^{3/5}$$

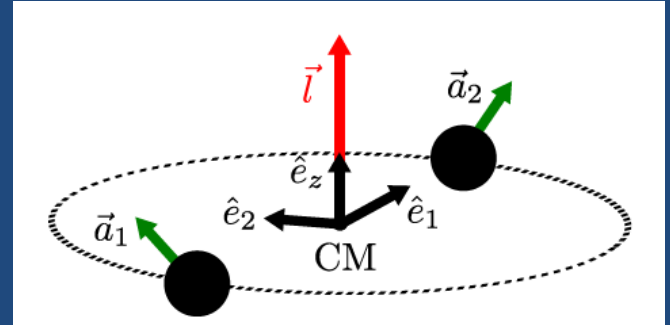
Parameters from GW observations

$$\mathcal{M} = \frac{(m_1 m_2)^{3/5}}{M^{1/5}}$$

Chirp mass

$$\chi_{\text{eff}} = \frac{(m_1 \vec{\chi}_1 + m_2 \vec{\chi}_2) \cdot \hat{L}_N}{M}$$

Effective spin

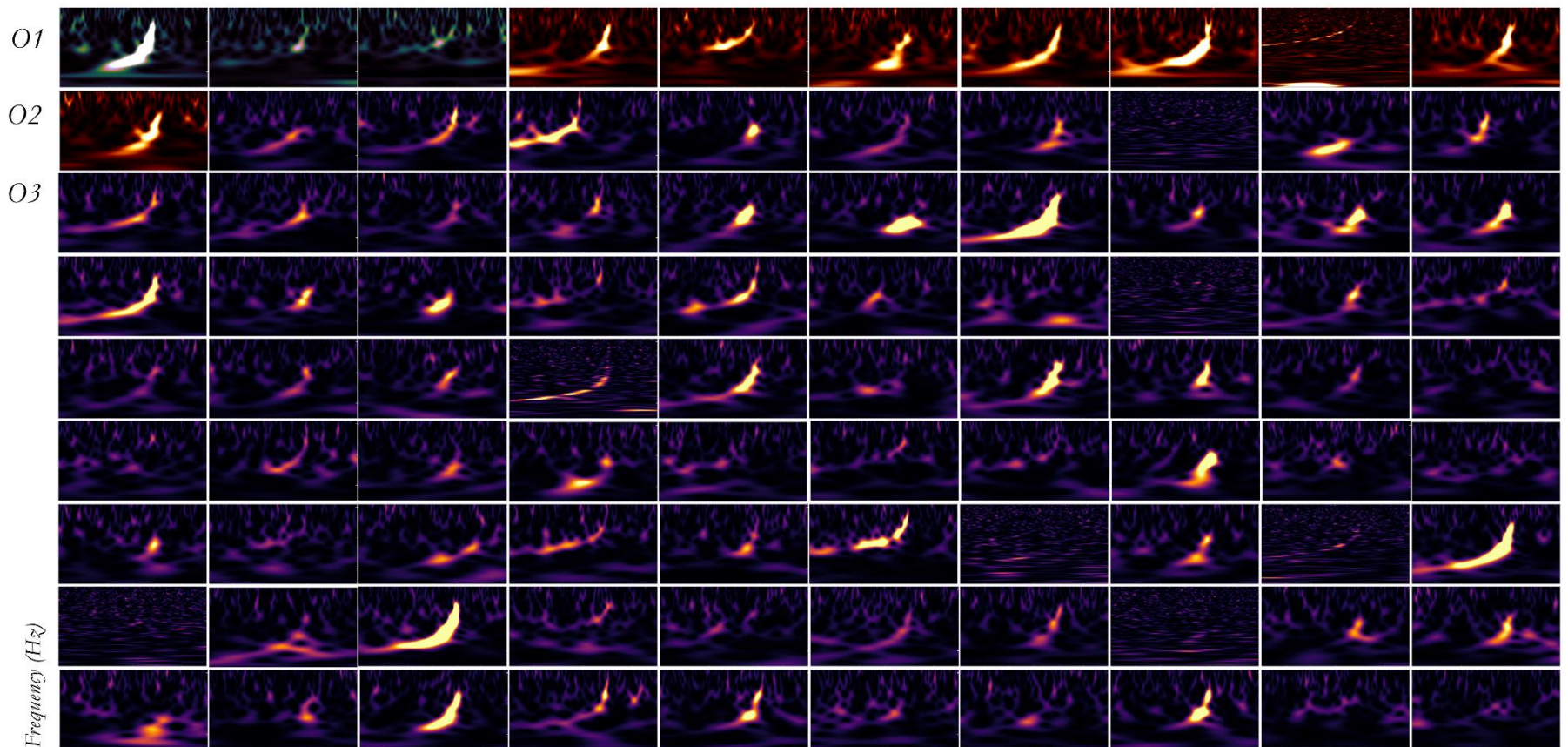


Event	m_1/M_\odot	m_2/M_\odot	\mathcal{M}/M_\odot	χ_{eff}	M_f/M_\odot	a_f	$E_{\text{rad}}/(M_\odot c^2)$	$\ell_{\text{peak}}/(\text{erg s}^{-1})$	d_L/Mpc	z	$\Delta\Omega/\text{deg}^2$
GW150914	$35.6^{+4.8}_{-3.0}$	$30.6^{+3.0}_{-4.4}$	$28.6^{+1.6}_{-1.5}$	$-0.01^{+0.12}_{-0.13}$	$63.1^{+3.3}_{-3.0}$	$0.69^{+0.05}_{-0.04}$	$3.1^{+0.4}_{-0.4}$	$3.6^{+0.4}_{-0.4} \times 10^{56}$	430^{+150}_{-170}	$0.09^{+0.03}_{-0.03}$	180
GW151012	$23.3^{+14.0}_{-5.5}$	$13.6^{+4.1}_{-4.8}$	$15.2^{+2.0}_{-1.1}$	$0.04^{+0.28}_{-0.19}$	$35.7^{+9.9}_{-3.8}$	$0.67^{+0.13}_{-0.11}$	$1.5^{+0.5}_{-0.5}$	$3.2^{+0.8}_{-1.7} \times 10^{56}$	1060^{+540}_{-480}	$0.21^{+0.09}_{-0.09}$	1555
GW151226	$13.7^{+8.8}_{-3.2}$	$7.7^{+2.2}_{-2.6}$	$8.9^{+0.3}_{-0.3}$	$0.18^{+0.20}_{-0.12}$	$20.5^{+6.4}_{-1.5}$	$0.74^{+0.07}_{-0.05}$	$1.0^{+0.1}_{-0.2}$	$3.4^{+0.7}_{-1.7} \times 10^{56}$	440^{+180}_{-190}	$0.09^{+0.04}_{-0.04}$	1033
GW170104	$31.0^{+7.2}_{-5.6}$	$20.1^{+4.9}_{-4.5}$	$21.5^{+2.1}_{-1.7}$	$-0.04^{+0.17}_{-0.20}$	$49.1^{+5.2}_{-3.9}$	$0.66^{+0.08}_{-0.10}$	$2.2^{+0.5}_{-0.5}$	$3.3^{+0.6}_{-0.9} \times 10^{56}$	960^{+430}_{-410}	$0.19^{+0.07}_{-0.08}$	924
GW170608	$10.9^{+5.3}_{-1.7}$	$7.6^{+1.3}_{-2.1}$	$7.9^{+0.2}_{-0.2}$	$0.03^{+0.19}_{-0.07}$	$17.8^{+3.2}_{-0.7}$	$0.69^{+0.04}_{-0.04}$	$0.9^{+0.05}_{-0.1}$	$3.5^{+0.4}_{-1.3} \times 10^{56}$	320^{+120}_{-110}	$0.07^{+0.02}_{-0.02}$	396
GW170729	$50.6^{+16.6}_{-10.2}$	$34.3^{+9.1}_{-10.1}$	$35.7^{+6.5}_{-4.7}$	$0.36^{+0.21}_{-0.25}$	$80.3^{+14.6}_{-10.2}$	$0.81^{+0.07}_{-0.13}$	$4.8^{+1.7}_{-1.7}$	$4.2^{+0.9}_{-1.5} \times 10^{56}$	2750^{+1350}_{-1320}	$0.48^{+0.19}_{-0.20}$	1033
GW170809	$35.2^{+8.3}_{-6.0}$	$23.8^{+5.2}_{-5.1}$	$25.0^{+2.1}_{-1.6}$	$0.07^{+0.16}_{-0.16}$	$56.4^{+5.2}_{-3.7}$	$0.70^{+0.08}_{-0.09}$	$2.7^{+0.6}_{-0.6}$	$3.5^{+0.6}_{-0.9} \times 10^{56}$	990^{+320}_{-380}	$0.20^{+0.05}_{-0.07}$	340
GW170814	$30.7^{+5.7}_{-3.0}$	$25.3^{+2.9}_{-4.1}$	$24.2^{+1.4}_{-1.1}$	$0.07^{+0.12}_{-0.11}$	$53.4^{+3.2}_{-2.4}$	$0.72^{+0.07}_{-0.05}$	$2.7^{+0.4}_{-0.3}$	$3.7^{+0.4}_{-0.5} \times 10^{56}$	580^{+160}_{-210}	$0.12^{+0.03}_{-0.04}$	87
GW170817	$1.46^{+0.12}_{-0.10}$	$1.27^{+0.09}_{-0.09}$	$1.186^{+0.001}_{-0.001}$	$0.00^{+0.02}_{-0.01}$	≤ 2.8	≤ 0.89	≥ 0.04	$\geq 0.1 \times 10^{56}$	40^{+10}_{-10}	$0.01^{+0.00}_{-0.00}$	16
GW170818	$35.5^{+7.5}_{-4.7}$	$26.8^{+4.3}_{-5.2}$	$26.7^{+2.1}_{-1.7}$	$-0.09^{+0.18}_{-0.21}$	$59.8^{+4.8}_{-3.8}$	$0.67^{+0.07}_{-0.08}$	$2.7^{+0.5}_{-0.5}$	$3.4^{+0.5}_{-0.7} \times 10^{56}$	1020^{+430}_{-360}	$0.20^{+0.07}_{-0.07}$	39
GW170823	$39.6^{+10.0}_{-6.6}$	$29.4^{+6.3}_{-7.1}$	$29.3^{+4.2}_{-3.2}$	$0.08^{+0.20}_{-0.22}$	$65.6^{+9.4}_{-6.6}$	$0.71^{+0.08}_{-0.10}$	$3.3^{+0.9}_{-0.8}$	$3.6^{+0.6}_{-0.9} \times 10^{56}$	1850^{+840}_{-840}	$0.34^{+0.13}_{-0.14}$	1651

Coalescing binaries LIGO/Virgo

Gravitational-Wave Transient Catalog

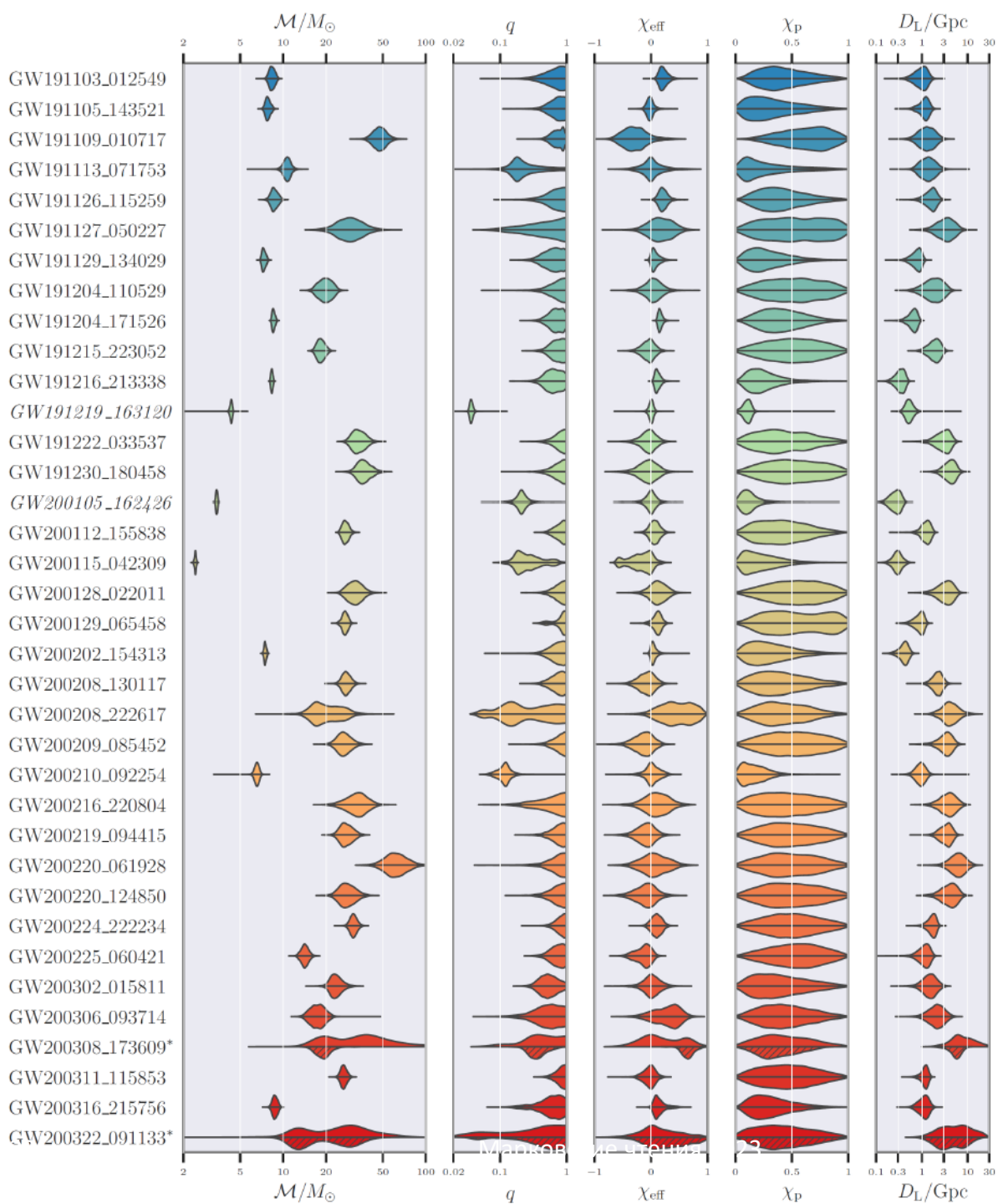
Detections from 2015-2020 of compact binaries with black holes & neutron stars



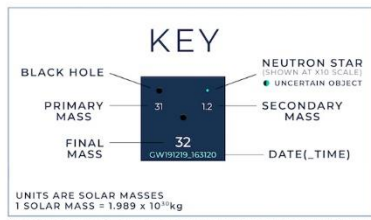
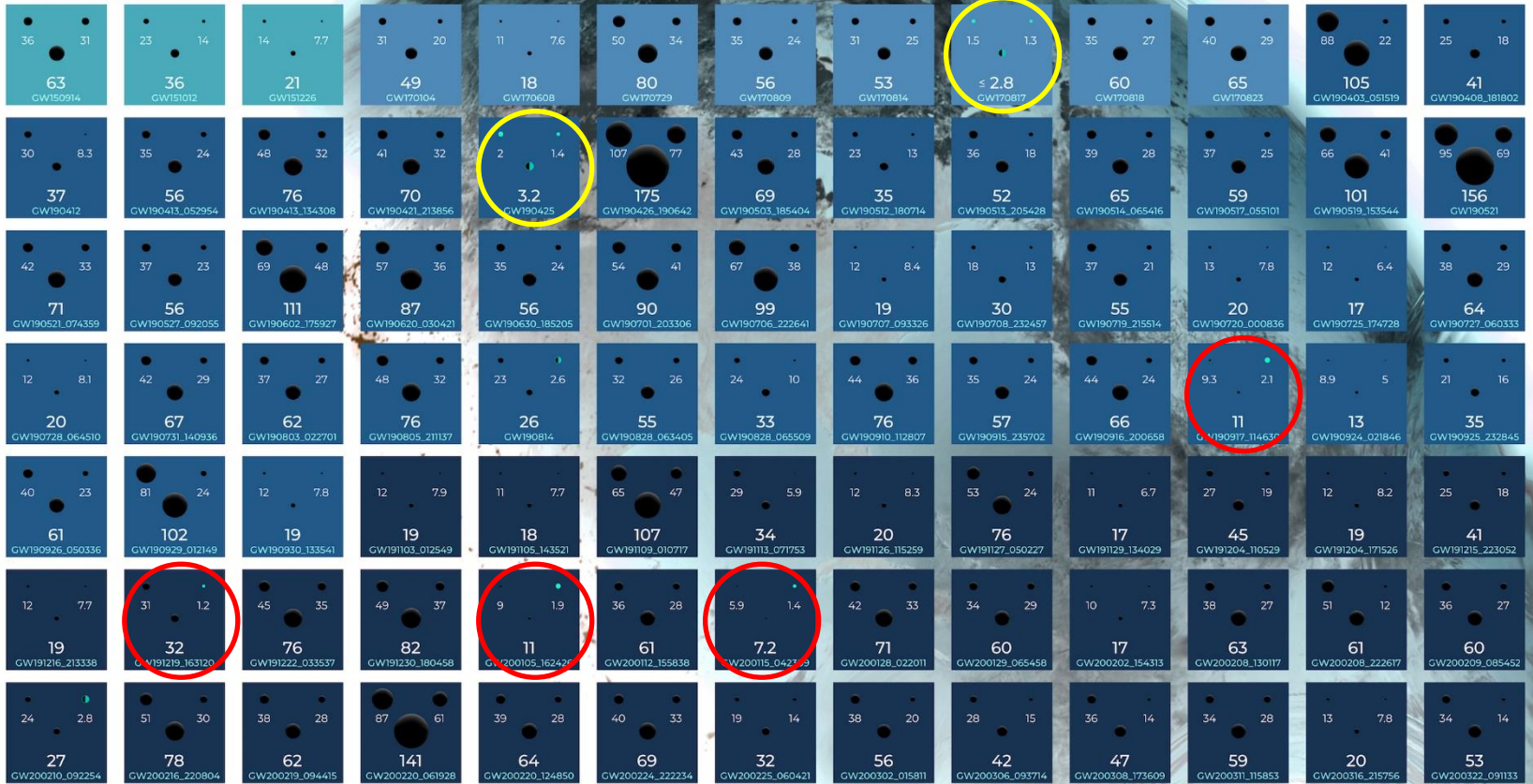
Time (s)

Sudarshan Ghonge | Karan Jani





- BBH
- BBH
- BBH
- BBH
- BBH
- BBH
- BBH
- BBH
- BBH
- BBH
- BBH
- NSBH
- BBH
- BBH
- NSBH
- BBH
- NSBH
- BBH
- BBH
- BBH
- BBH
- NSBH / BBH
- BBH
- BBH
- BBH
- BBH
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- BBH
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- BBH
- BBH
- BBH
- BBH
- BBH



Note that the mass estimates shown here do not include uncertainties, which is why the final mass is sometimes larger than the sum of the primary and secondary masses. In actuality, the final mass is smaller than the primary plus the secondary mass.

The events listed here pass one of two thresholds for detection. They either have a probability of being astrophysical of at least 50%, or they pass a false alarm rate threshold of less than 1 per 3 years.

GRAVITATIONAL WAVE MERGER DETECTIONS

SINCE 2015

AIC Centre of Excellence for Gravitational Wave Discovery

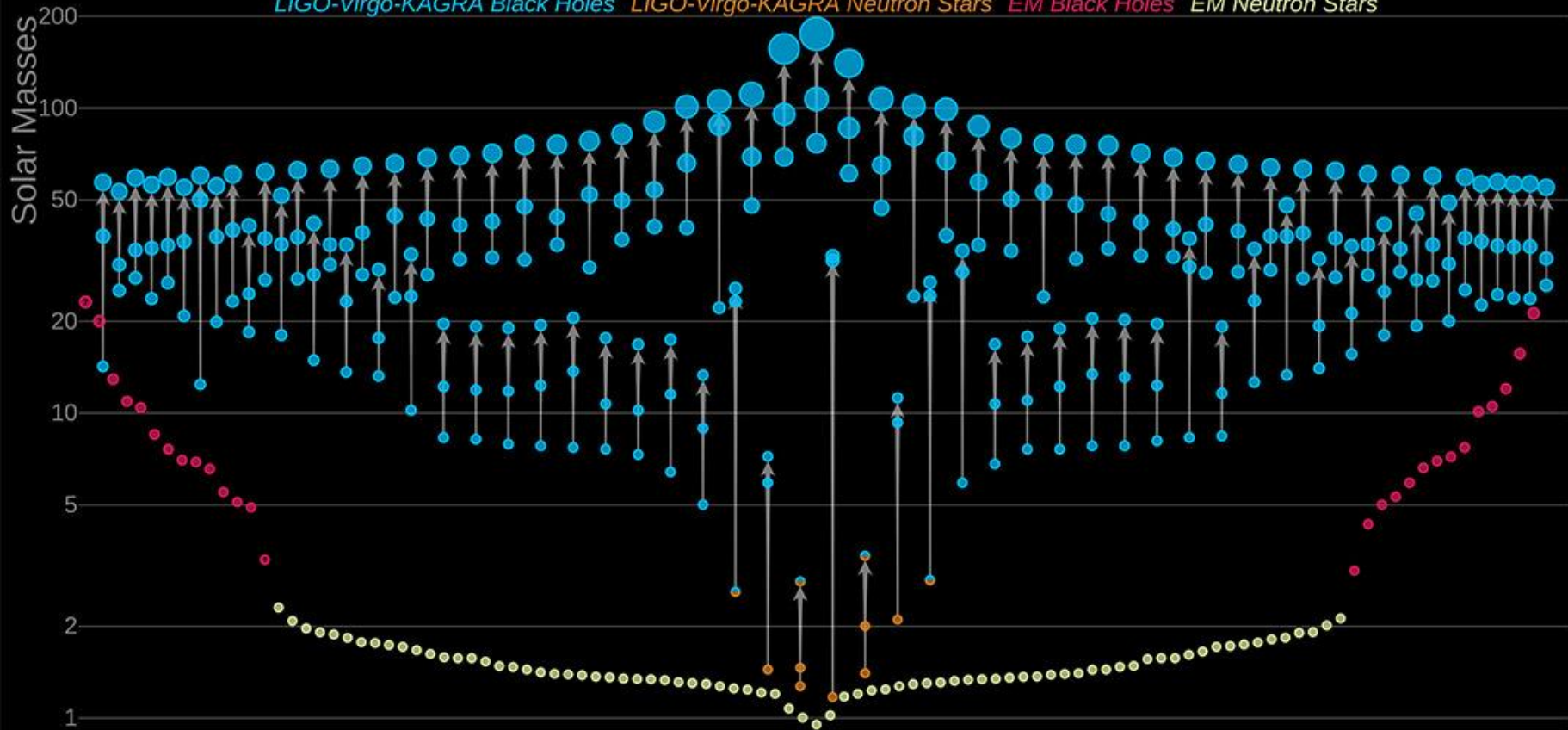


Statistical properties: summary

- O1+O2+O3: 91 robust ($S/N > 8$) detections
- Isotropic on the sky (2207.05792)
- Signal properties in agreement with GR up to a few % accuracy
- 2 NS+NS mergings, EM from GW 170817
- 4 BH+NS candidates. No electromagnetic signals.

Masses in the Stellar Graveyard

LIGO-Virgo-KAGRA Black Holes LIGO-Virgo-KAGRA Neutron Stars EM Black Holes EM Neutron Stars



LIGO-Virgo-KAGRA | Aaron Geller | Northwestern

Exceptional BHBH mergers

- **GW 190814**, $M_1=26$, $q=0.112$, $M_2=2.6$ in lower mass gap? NS? Strange quark star? Outlier population? Formation from a triple star? Formation in AGN disk? Primordial BH?
- **GW190521** $m_1 = 85^{+21}_{-14} M_\odot$ $m_2 = 66^{+17}_{-18} M_\odot$ in upper mass gap (60-120), large effective spin ($\chi_{1,2} \sim 0.1-0.9$)
(Or even $m_1 = 168^{+15}_{-61} M_\odot$ $m_2 = 66^{+33}_{-3} M_\odot$??)

Repeated mergers in stellar clusters or AGN disks?? Primordial BH?

- **GW190412** $m_1 = 30.1^{+4.6}_{-5.3} M_\odot$ $m_2 = 8.3^{+1.6}_{-0.9} M_\odot$ high spin $\chi_1 = 0.44^{+0.16}_{-0.22}$

→ Hierarchical merger?

GW190521 as hyperbolic encounter of non-spinning BHs?

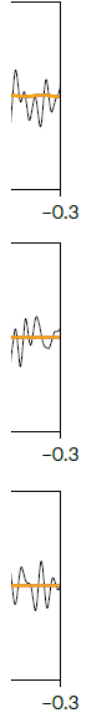
a

Table 1 | Source parameters of GW190521 with median values and 90% credible intervals quoted and natural logarithms reported

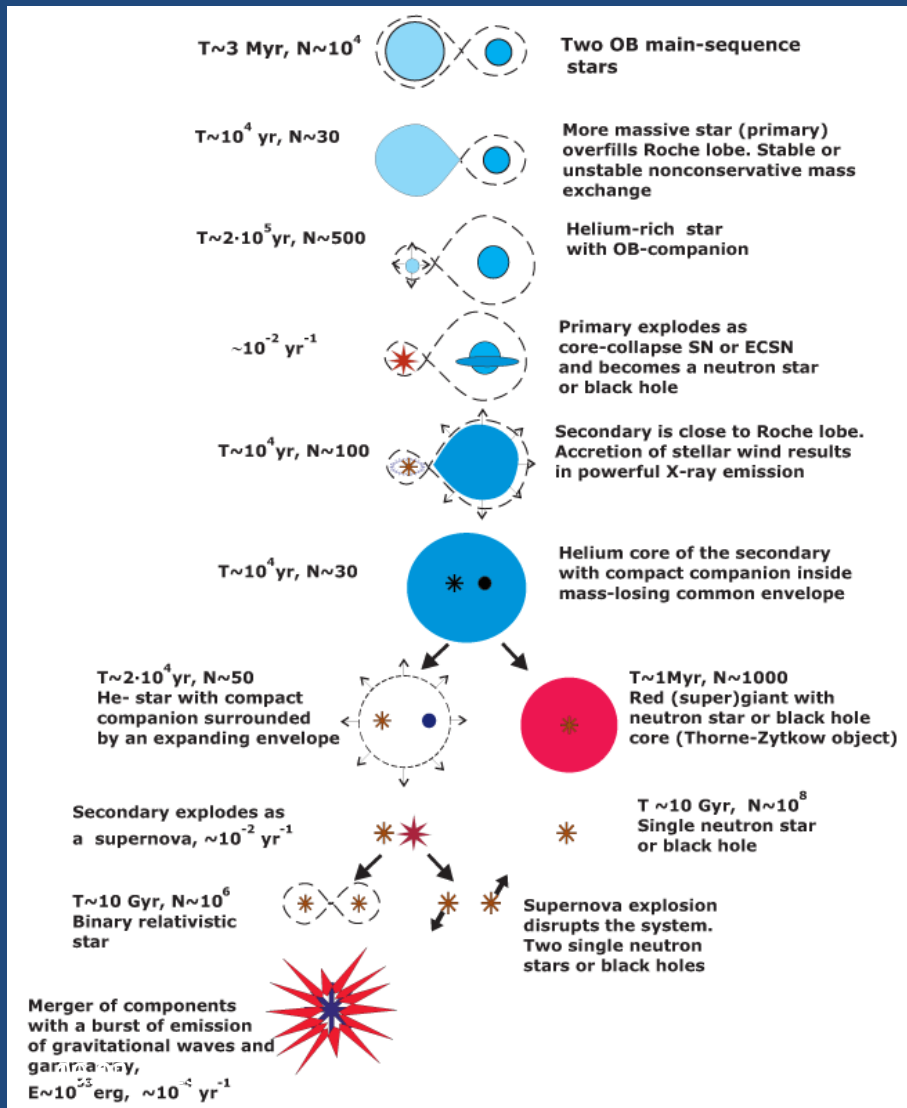
Reference ^a	This paper		LVK ⁴			Gayathri et al. ¹⁵	Romero-Shaw et al. ¹⁶	
Waveform	TEOBResumS ^{30,31}	TEOBResumS ^{30,31}	TEOBResumSP ^{44b}	NRSur7dq4 (ref. ⁴²)	NRSur7dq4 (ref. ⁴²)	NRSur7dq4 (ref. ⁴²)	NR ⁴⁷	SEOBNRE ⁵²
E_0 prior	Unconstrained (UE_0)		Constrained (CE_0)	-	-	-	-	-
Multipoles	$(\ell, m)=(2, 2)$		$(\ell, m)=(2, 2)$	$(\ell, m)=(2, 2)$	$\ell \leq 4$	$\ell \leq 4$	-	-
$m_1 (M_\odot)$	85^{+88}_{-22}	81^{+62}_{-25}	90^{+19}_{-14}	102^{+35}_{-23}	84^{+17}_{-12}	85^{+21}_{-14}	102^{+7}_{-11}	92^{+26}_{-16}
$m_2 (M_\odot)$	59^{+18}_{-37}	52^{+32}_{-32}	66^{+10}_{-8}	64^{+19}_{-25}	71^{+16}_{-18}	66^{+17}_{-18}	102^{+7}_{-11}	69^{+18}_{-19}
$M_{\text{source}} (M_\odot)^c$	151^{+73}_{-51}	130^{+75}_{-43}	156^{+25}_{-15}	164^{+40}_{-23}	153^{+29}_{-19}	150^{+29}_{-17}	-	-
$m_2/m_1 \leq 1$	$0.69^{+0.27}_{-0.52}$	$0.63^{+0.31}_{-0.43}$	$0.73^{+0.21}_{-0.15}$	$0.62^{+0.32}_{-0.30}$	$0.86^{+0.12}_{-0.30}$	$0.79^{+0.19}_{-0.29}$	-	-
χ_{eff}^d	-	-	$-0.05^{+0.09}_{-0.12}$	$0.01^{+0.24}_{-0.26}$	$-0.03^{+0.25}_{-0.26}$	$0.08^{+0.27}_{-0.36}$	0	$0.0^{+0.2}_{-0.2}$
χ_p^e	-	-	$0.72^{+0.16}_{-0.22}$	$0.71^{+0.22}_{-0.36}$	$0.79^{+0.16}_{-0.40}$	$0.68^{+0.25}_{-0.37}$	0.7	-
Eccentricity	-	-	-	-	-	-	0.67	0.11 ^f
E_0/M	$1.014^{+0.009}_{-0.012}$	$1.014^{+0.010}_{-0.012}$	-	-	-	-	-	-
p_φ^0	$4.18^{+0.50}_{-0.62}$	$4.24^{+0.57}_{-0.37}$	-	-	-	-	-	-
Luminosity distance D_L (Gpc)	$4.7^{+4.8}_{-2.7}$	$6.1^{+3.3}_{-3.7}$	$4.5^{+1.2}_{-1.2}$	$3.9^{+2.3}_{-1.9}$	$4.8^{+2.3}_{-2.2}$	$5.3^{+2.4}_{-2.6}$	$1.84^{+1.07}_{-0.054}$	$4.1^{+1.8}_{-1.8}$
SNR_{max}	15.2	15.4	14.7	14.7	14.6	15.4	-	-
$\log(L)_{\text{max}}$	123.2	123.0	106.0	107.0	105.6	-	-	-
$\log B_{\text{noise}}^{\text{signal}}$	84.00 ± 0.18	83.30 ± 0.18	72.95 ± 0.08	74.76 ± 0.11	74.86 ± 0.11	-	-	-

^aResults of other analyses^{41,516} are included for reference ^bSpin results obtained at a reference frequency of 5 Hz ^cTotal mass in the frame of the source ^dEffective spin along the orbital angular momentum ^eEffective precessing spin ^fLower limit at 10 Hz

180°



Principal sources: compact binary coalescences



Evolution of massive binaries

Tutukov, Yungelson 1993

Lipunov, Postnov, Prokhorov 1997

.....

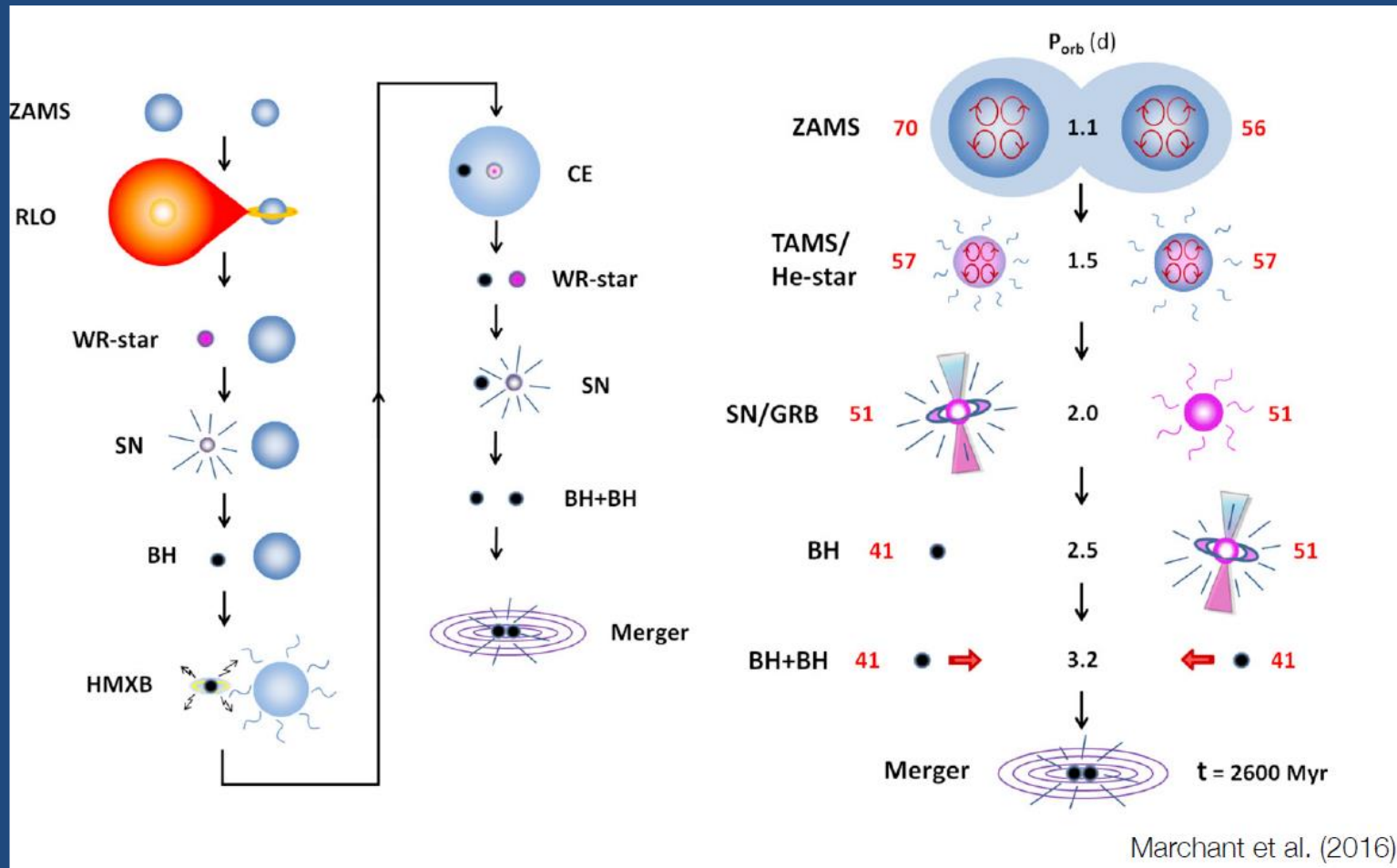
Other scenarios:

Dynamical interactions in stellar clusters

Exotica (primordial BHs)

...

Simplest scenario: BH+BH from massive star evolution

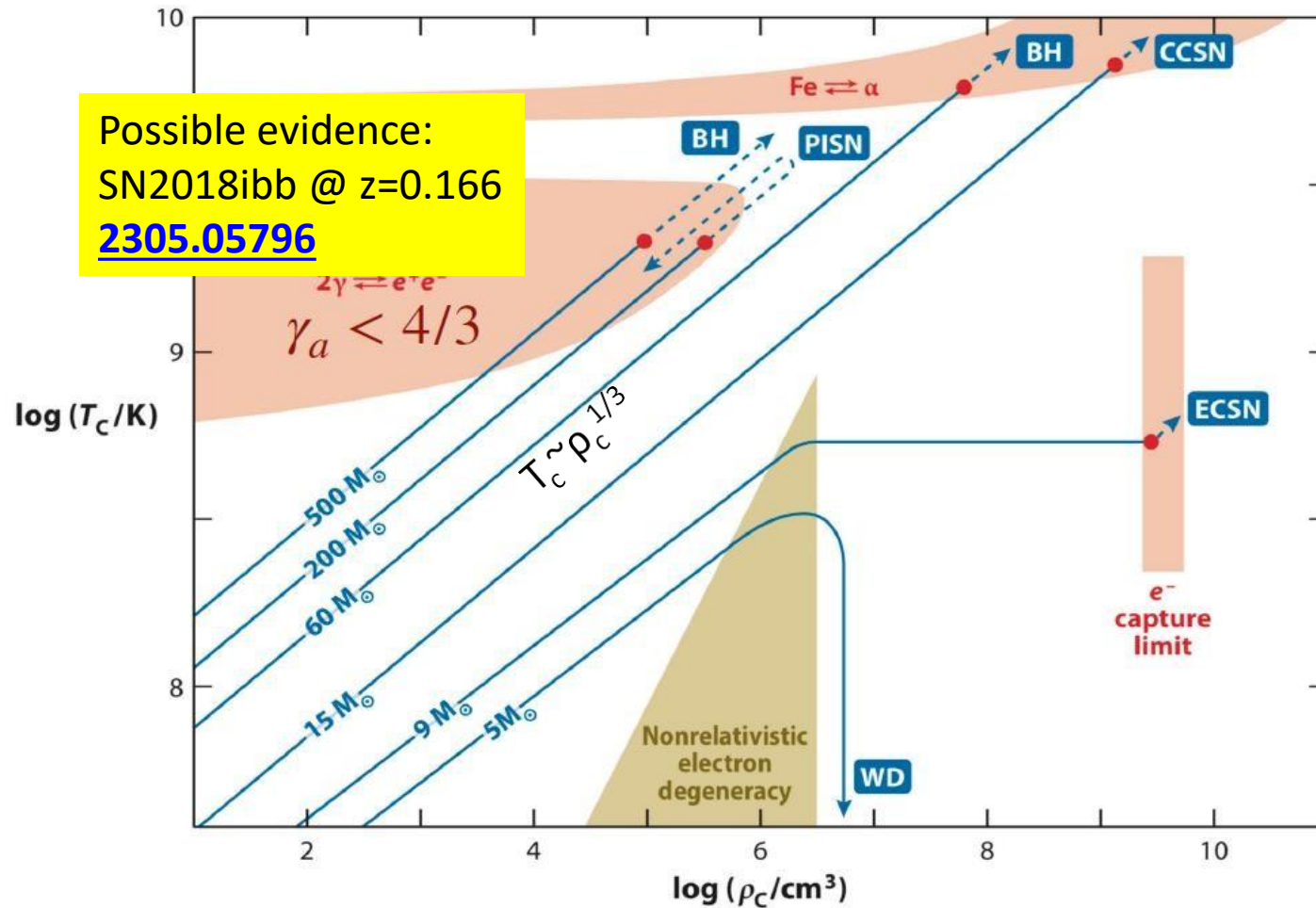


Astrophysical issues: BH from stellar collapses, binary BH formation

- Mass loss from massive stars
- BH mass gaps (2.5-5, 60-130 M_{sun})
- BH kicks
- BH spins
- ...

BH formation from stars

Possible evidence:
SN2018ibb @ z=0.166
[2305.05796](https://arxiv.org/abs/2305.05796)



Langer (2012)

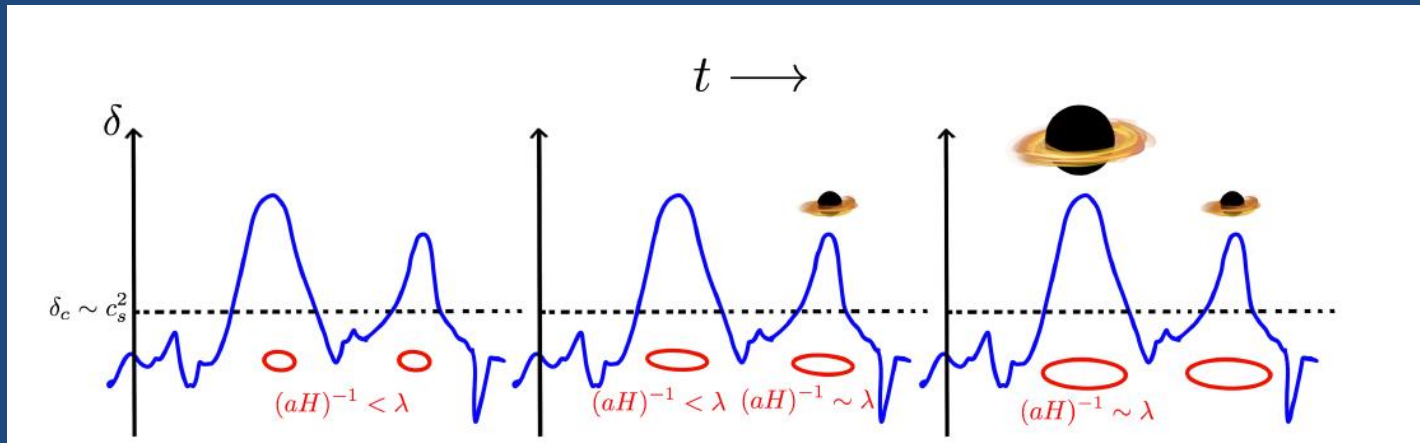
Possible astrophysical explanations of most massive LIGO binaries

- GW measurement uncertainty (straddling the gap: 2009.05742)
- Dynamical formation in dense stellar cluster (signs of large pre-merging eccentricity: 2009.04771), repeated mergers (3: 2009.05065, 7: 2010:0616)
- Population III stars (BH mass up to $75 M_{\odot}$: 2009.06585; up to $150 M_{\odot}$: 2009.06922, 2009.11447; direct collapse $90 \rightarrow 90$ for small convection overshooting: 2010:07616)
- Accretion growth in dense molecular clouds (2009.11326)
- Standard low-Z binary evolution with direct collapse (BH mass up to $90 M_{\odot}$: 2009.13526)
- Addition of additional nuclear energy (DM?) to avoid PISN ($M_{\text{BH}} \sim 120 M_{\odot}$: 2010.00245)
- Stellar merger of low-Z stars to avoid mass gap (2010.00705)
- Stellar physics of PISN (shifting the gap to $92\text{-}110 M_{\odot}$: 2010.02242)

Other scenarios

Dynamical capture in dens stellar clusters (can produce BH with $M > 50 M_{\odot}$ and non-parallel BH spins)

- “Exotic” scenarios – primordial BH
(Zeldovich, Novikov 1967... Carr 1975... Dolgov & Silk 1993...)



LIGO BH+BH: Could they be PBH?

- Stellar-mass **primordial black holes**:
 - Can be formed in the early Universe in different models (Zeldovich, Novikov'67, Carr, Hawking'74)
 - Can be in binaries (Nakamura+'97)
 - Can naturally explain observed BH+BH rate (Bird+'16, Blinnikov+'16, Sasaki+'16...)
 - Can substantially contribute to dark matter
 - Can be seeds for growth of SMBH in galactic centers

Binary PBH formation

- At some z more than one PBH is inside the Hubble horizon:

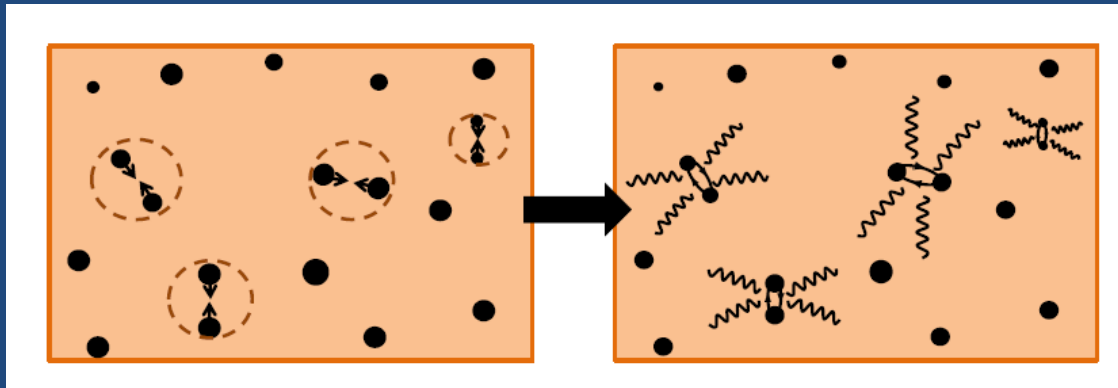
$$H(z)\ell_{\text{PBH}}(z) = H(z)n_{\text{PBH}}^{-1/3}(1+z)^{-1} \simeq 6 \times 10^{-6} f_{\text{PBH}}^{-1/3} \left(\frac{1+z}{1+z_{\text{eq}}} \right) \left(\frac{M_{\text{PBH}}}{30 M_{\odot}} \right)^{1/3}$$

$$z_{\text{eq}} \sim 10^4$$

- Decoupling from the Hubble flow at

$$1 + z_{\text{dec}} = (1 + z_{\text{eq}}) \left(\frac{x_{\text{max}}}{x} \right)^3$$

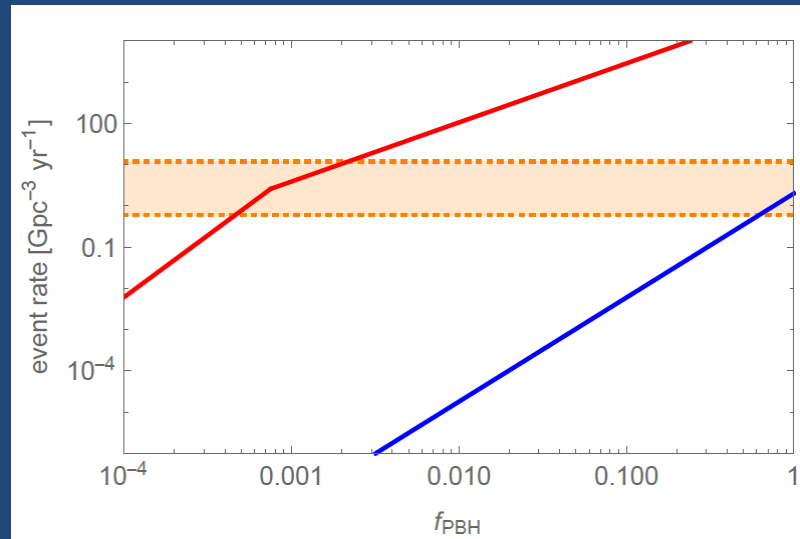
$$x < x_{\text{max}} \equiv f_{\text{PBH}}^{1/3} \ell_{\text{PBH}}(z=0)$$



Merging rate (model-dependent)

$$\mathcal{R} = n_{\text{PBH}} \frac{dP}{dt} = \frac{3n_{\text{PBH}}}{58} \left(\frac{t}{T}\right)^{\frac{3}{8}} \left[\frac{1}{(1 - e_{\text{upper}}^2)^{\frac{25}{16}}} - 1 \right] \frac{1}{t}$$

Sazaki+'16



f_{pbh} can be $\sim O(1)$
for PBH in clusters
(Eroshenko, Stasenko 2302.06157)

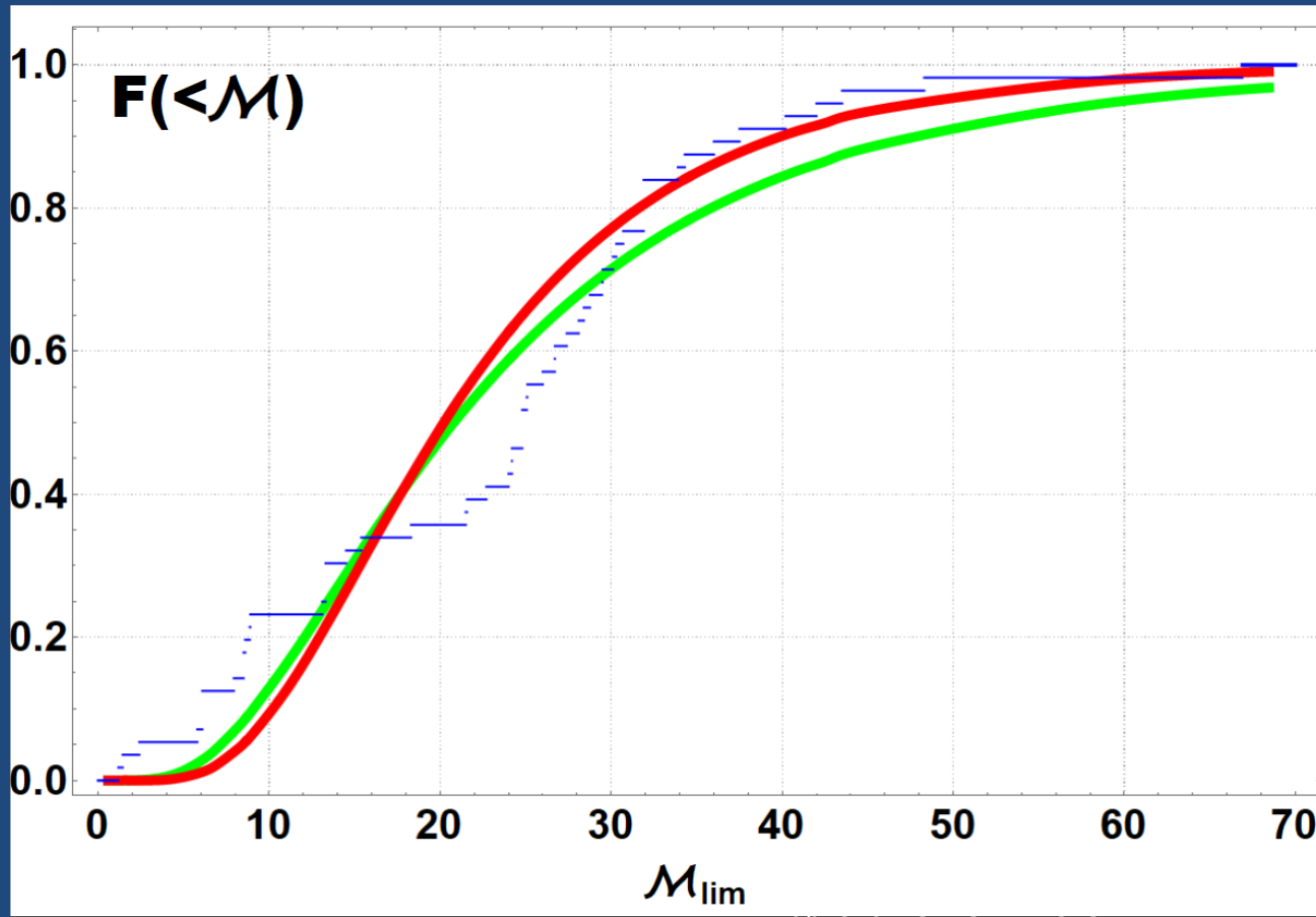
$$dR_0 = \frac{1.6 \times 10^6}{\text{Gpc}^3 \text{ yr}} f_{\text{PBH}}^{\frac{53}{37}} \eta^{-\frac{34}{37}} \left(\frac{M}{M_{\odot}}\right)^{-\frac{32}{37}} \left(\frac{t}{t_0}\right)^{-\frac{34}{37}} \psi(m_1) \psi(m_2) dm_1 dm_2$$

$$\psi(m) = \frac{1}{\sqrt{2\pi\sigma m}} \exp\left(-\frac{\ln^2(m/m_c)}{2\sigma^2}\right)$$

Raidal+'17

Example: log-normal PBH mass function GWTC1+GWTC2

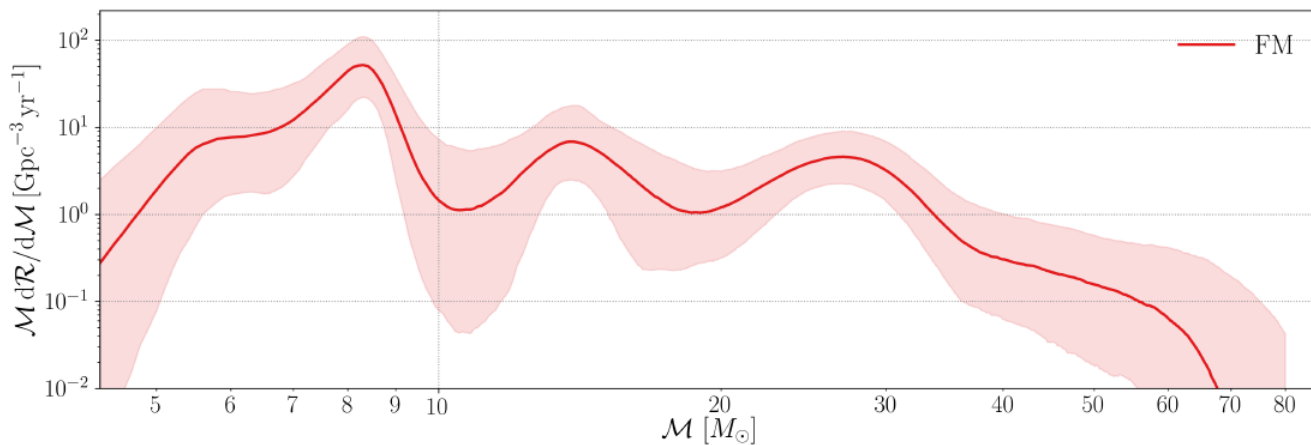
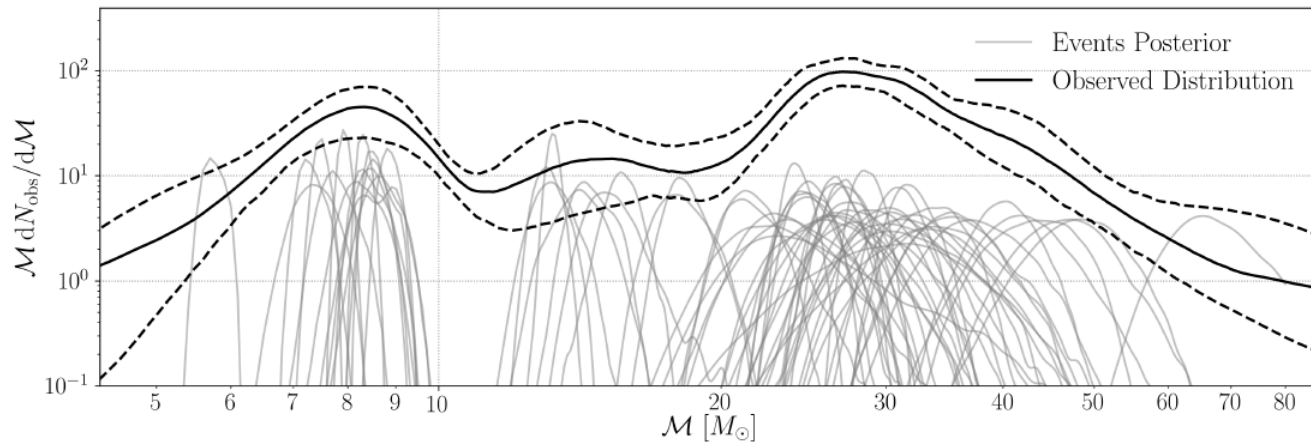
$$F(M) = A \exp[-\gamma \ln^2(M/M_0)]$$



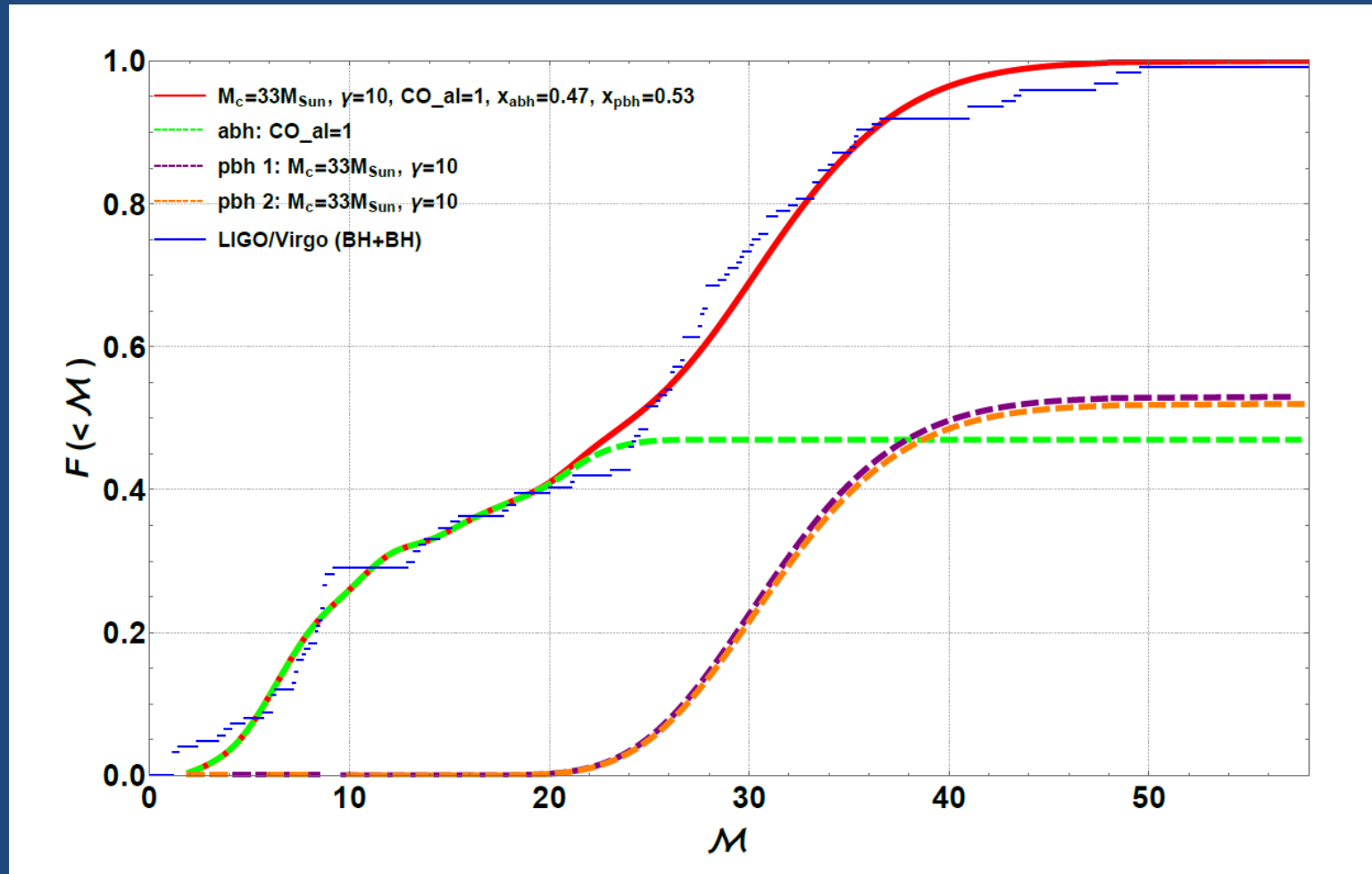
$$\gamma = 0.7, M_0 = 19$$

$$DR(M_{ch})dM_{ch} \sim A e^{-B \ln^2\left(\frac{M_{ch}}{M_0}\right)} dM_{ch}$$

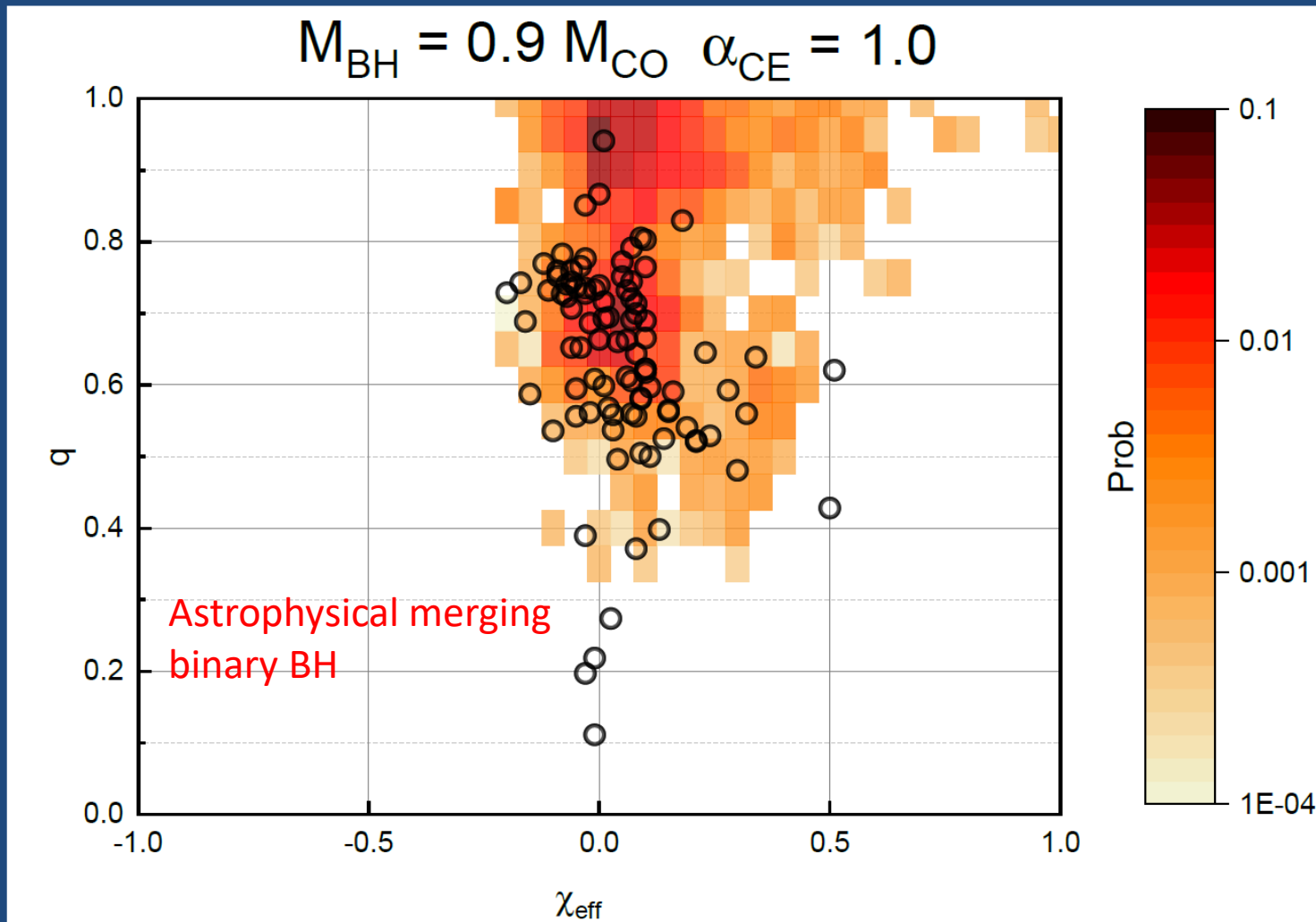
GWTC-3 features



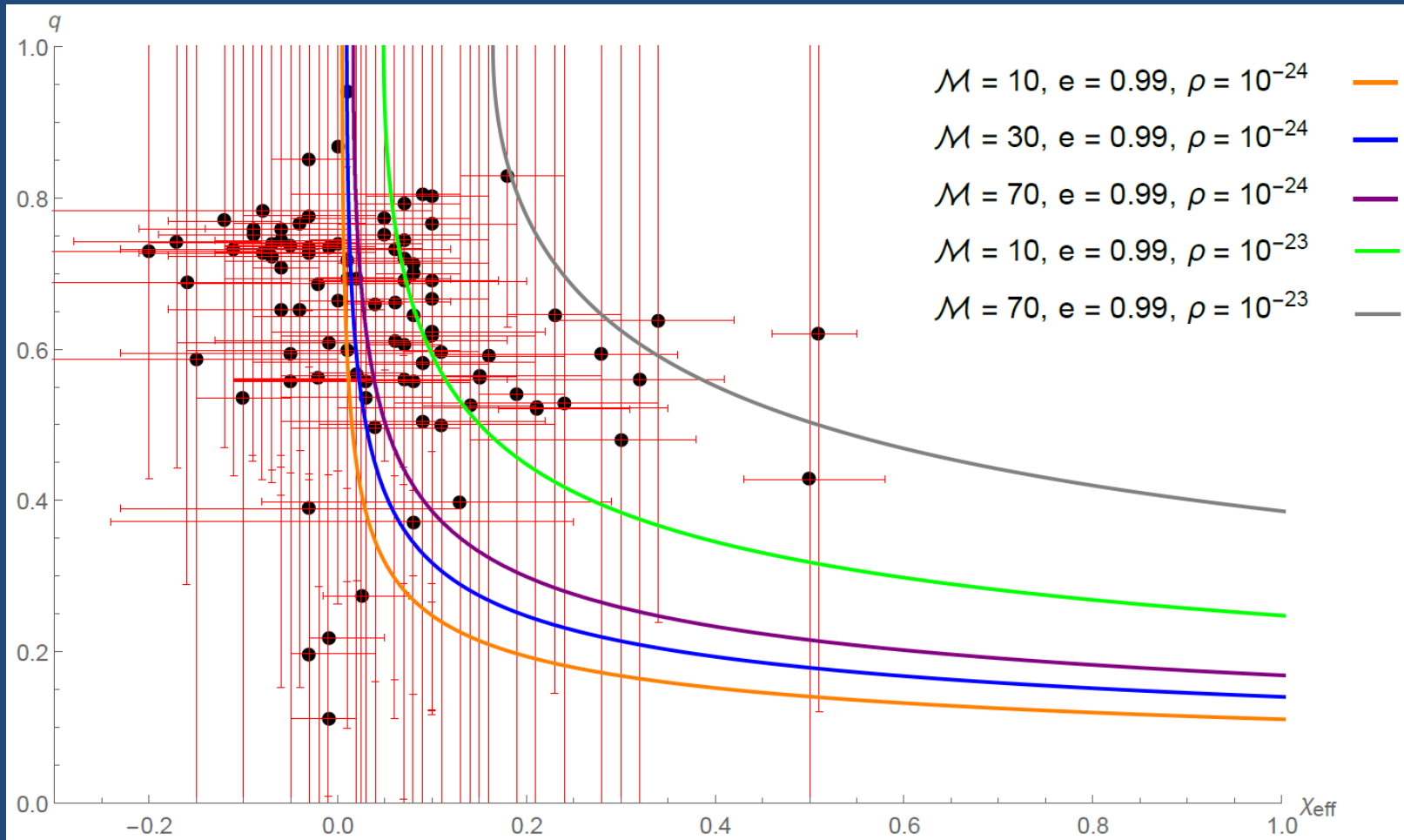
Astrophysical BHs +PBHs in GWTC-3



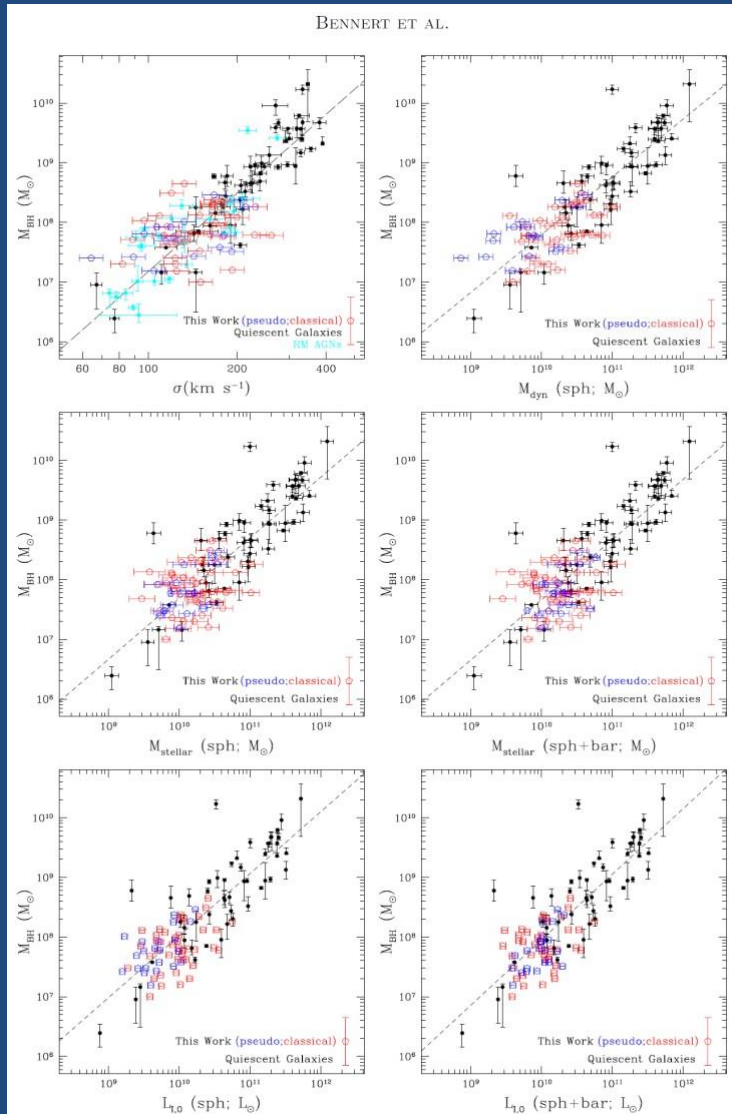
Effective spin – mass ratio correlation?



Accretion induced spin in eccentric PBH binaries



II. SMBH Astronomy



- $M \sim \sigma^4$
- $M \sim M_{\text{sph}}$
- $M \sim L_{\text{sph}}$

2101.10355

SMBH records

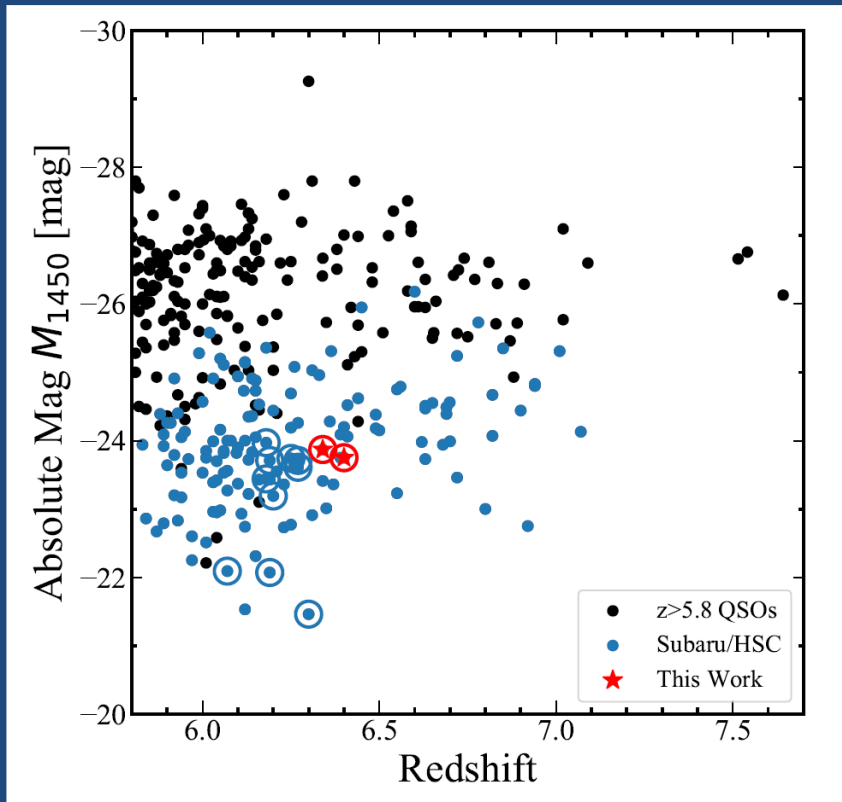
- >200 QSOs @ $z > 6$, ~a few @ $z > 7$ (700 mln yrs)

Source	z	M/M_{\odot}
SDSS J0100+2802	6.3	1.2×10^{10}
J1007+2115	7.52	1.5×10^9
ULAS J1342+0928	7.54	7.8×10^8
J0313-1806	7.62	1.6×10^9

- $L \sim 0.6 L_{\text{edd}}$, SFR $\sim 200 M_{\odot}$ per year ($\sim 100 \times \text{MW}$)

- Require BH seeds $> 100-10^5 M_{\odot}$ 2006.13452
2101.03179

High-redshift QSOs and SMBH growth



- >200 QSO $z > 6$
- Central SMBH $M \sim 10^9 M_{\odot}$
- Inefficient merging
- Eddington-limited accretion
- Need for 'massive 'seeds'
 $M \sim 10^3 - 10^4 M_{\odot}$
- Population III star?
Primordial massive BHs?

2211.14329

JWST

[2303.15431](#)

Spectroscopy of bright, early galaxy candidates 5

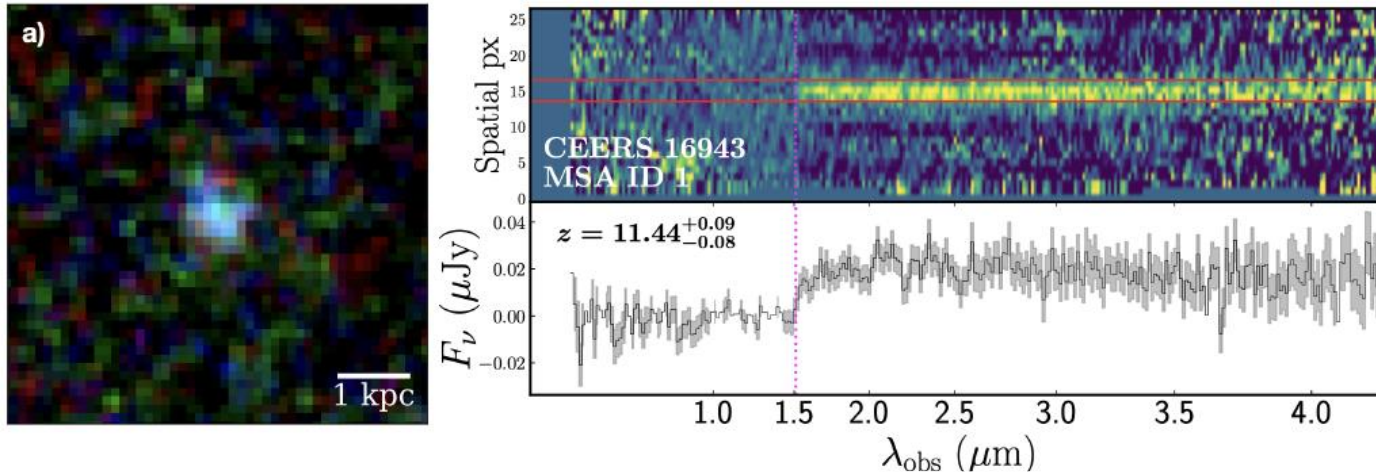
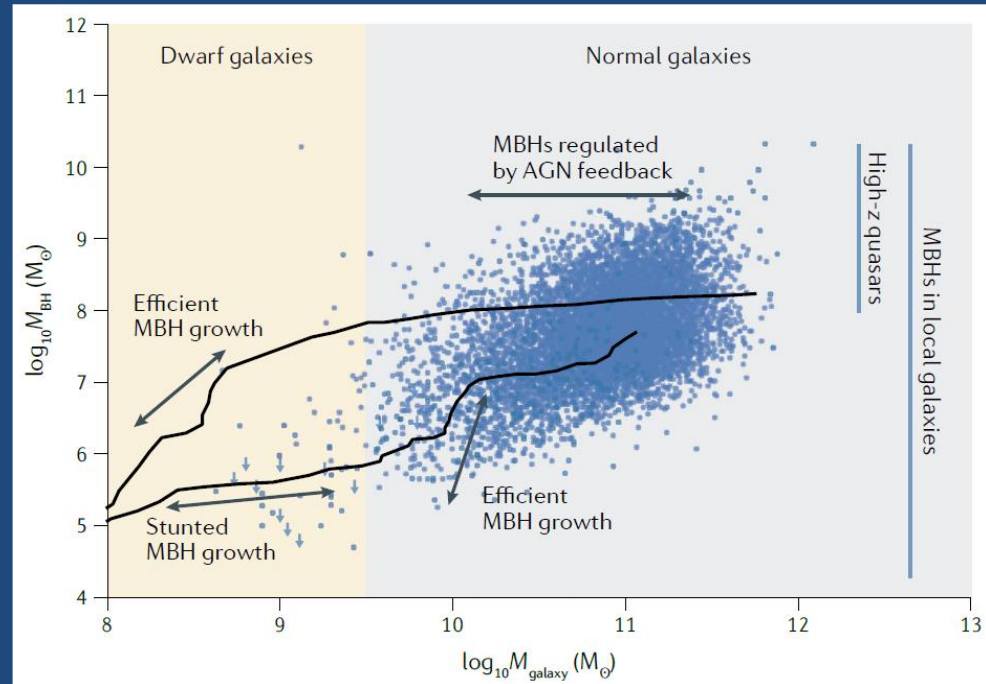
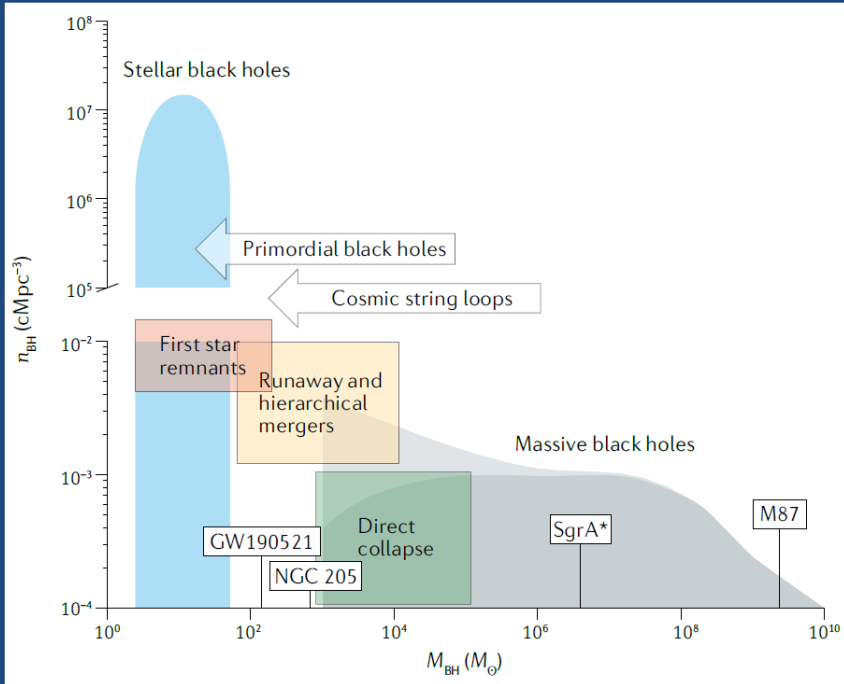


Fig. 2 a) A color image of Maisie’s Galaxy, showing a color (made from the F277W, F356W, and F444W images) of low dust attenuation and a fairly young stellar population. b) Maisie’s Galaxy’s spectrum around the detected Ly α break. The bright trace, with the negative “shadows” represent nodules. The red horizontal lines show the spatial extent in the bottom panel, was extracted. A clear spectral break is seen with significant flux. We interpret this as the Ly α break at a time 390 Myr after the Big Bang.

Property	Maisie’s Galaxy
RA (J2000)	214.943152
Dec (J2000)	52.942442
Photometric Redshift	$11.08^{+0.36}_{-0.39}$
Spectroscopic Redshift	$11.44^{+0.09}_{-0.08}$
$\mathcal{T}_{\text{BigBang}}$ (Myr)	391
$\log(M_\star/M_\odot)$	$8.4^{+0.3}_{-0.4}$
A_V (mag)	$0.07^{+0.09}_{-0.05}$
$\log(\text{sSFR}/\text{yr}^{-1})$	$-8.0^{+0.4}_{-0.5}$

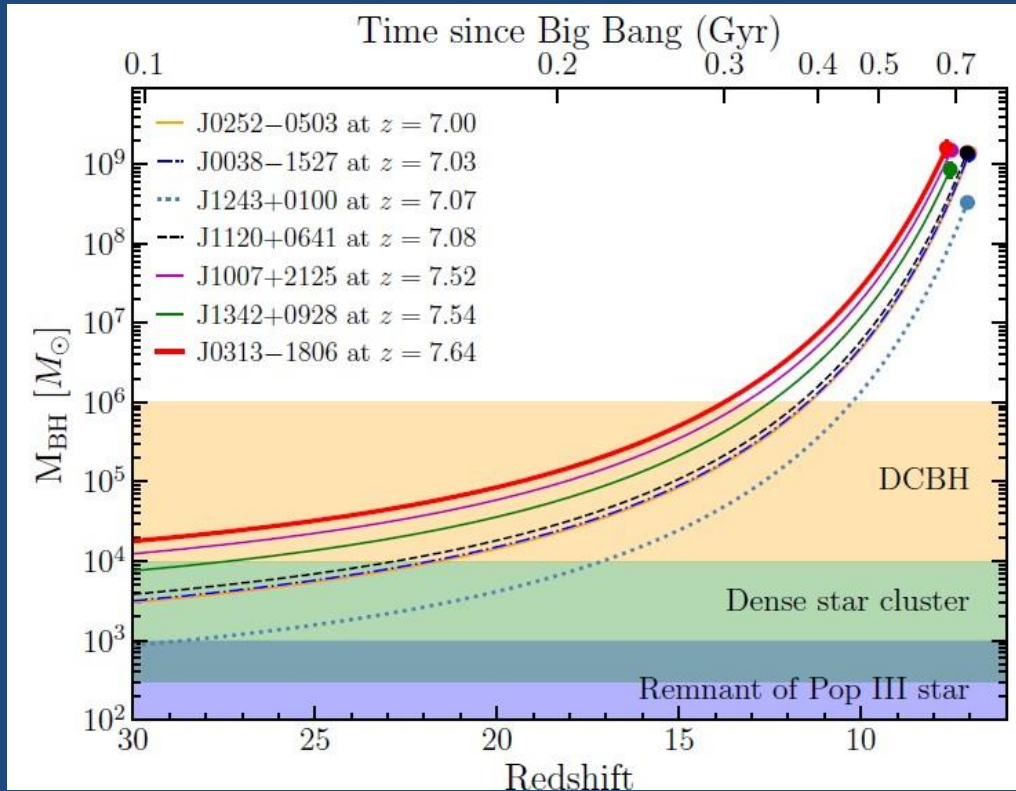
Massive BH formation



Massive BH seeds can outshine their host galaxies in far IR and mm!

Volonteri + '21

SMBH mass growth



Massive
PBH seeds?

2101.03179,
2012.01458

$$M_{\text{BH}}(t) = M_{\text{seed}} \times \exp\left(\frac{t - t_{\text{form}}}{t_{\text{Sal}}} \delta l_{\text{E}}\right)$$

$$t_{\text{Sal}} = \frac{\kappa_{\text{e.s.c}}}{4\pi G} \frac{\epsilon}{1 - \epsilon} \simeq 45 \frac{\epsilon}{0.1} \frac{0.9}{1 - \epsilon} \text{Myr}$$

Conclusions

- LVK O1+O2+O3: ~ 91 detections of binary BH and NS mergings, mostly binary BH, rate $\sim 10\text{-}200 \text{ Gpc}^{-3} \text{ yr}^{-1}$
 - **Astrophysical problems** in formation of massive BH with $M \sim 100 M_{\odot}$, extreme mass ratio BH+BH inspirals, BH+NS
 - **Possibility of $\sim 10+ M_{\odot}$ PBH is still open!**
- LIGO, Virgo, and KAGRA are closely coordinating to start the O4 Observing run together on **May 24 2023**.
 - **LIGO** sensitivity goal of **160-190 Mpc** for binary neutron stars. **Virgo** target sensitivity of **80-115 Mpc**. **KAGRA** should be running with greater than **1 Mpc** sensitivity at the beginning of O4, and will work to improve the sensitivity toward the end of O4.
- $\sim 10^4+ M_{\odot}$ PBH as seeds of high-redshift galaxies

Backup slides

Mass-redshift degeneracy

$$f_o = f / (1 + z), \quad dt_o = dt(1 + z)$$

$$\left. \frac{df}{dt} \right|_o = \frac{df}{dt} \frac{1}{(1 + z)^2}$$

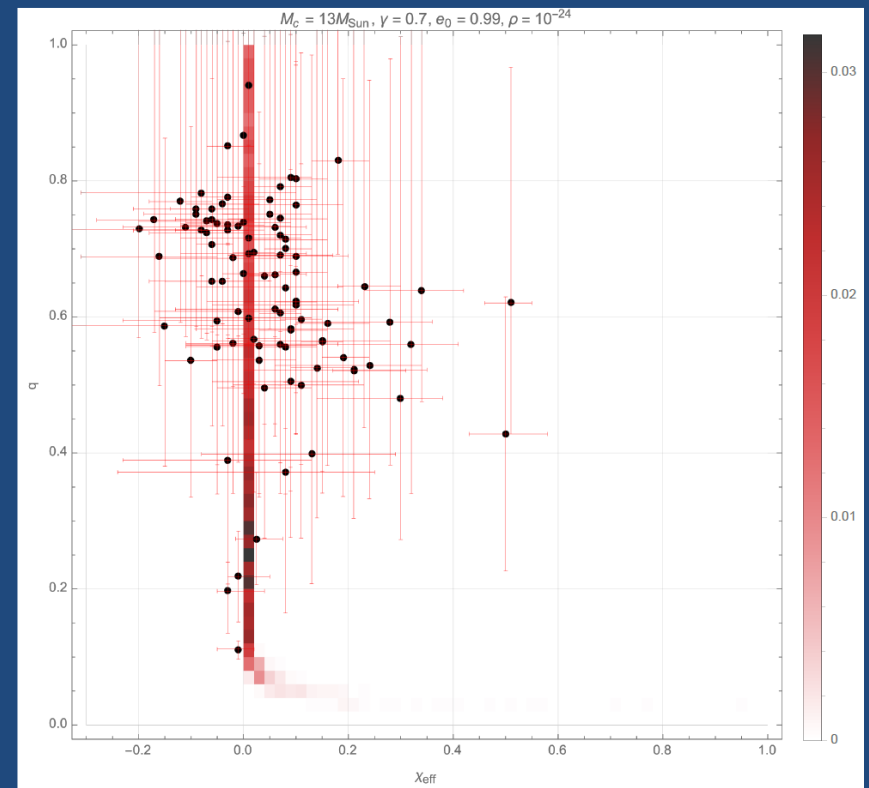
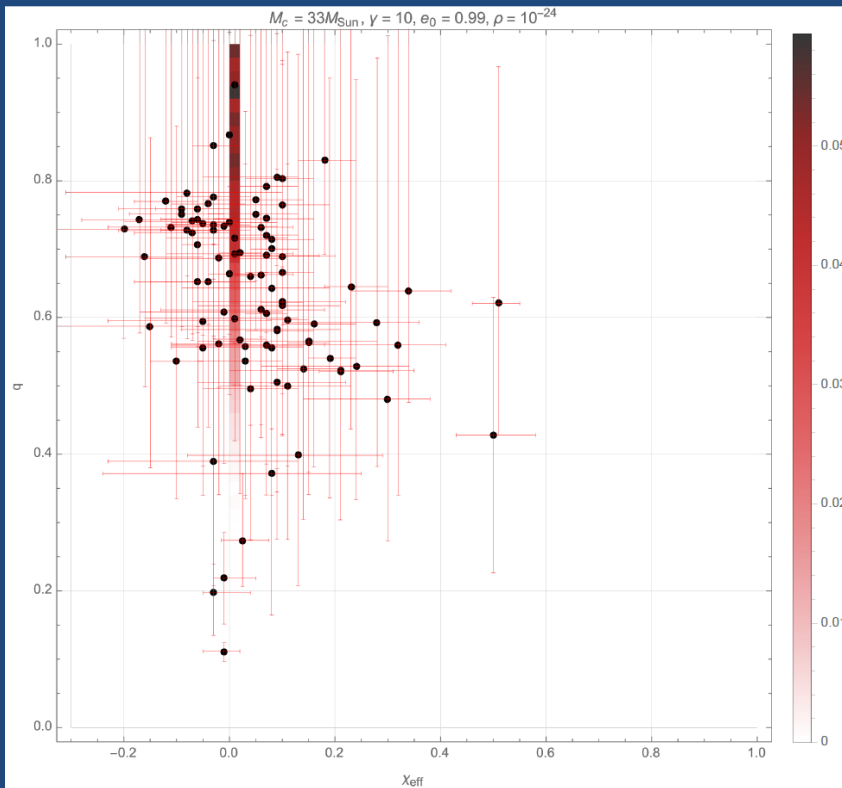
$$M_{ch}|_o = \left(\frac{5 f_o^{-11/3} (df_o / dt)}{96 \pi^{8/3}} \right)^{3/5} = M_{ch} (1 + z) \implies f M_{ch} = \text{inv}$$

$$h_o \sim \frac{M_{ch}}{d_m} (\pi f M_{ch})^{2/3}$$

$$d_o \sim \frac{4(M_{ch})_o}{h_o} (\pi f_o (M_{ch})_o)^{2/3} = d_m (1 + z)$$

Luminosity distance

Binary merging PBH



Chirp mass determines detection horizon. $h_{\text{lim}} \sim M^{(5/6)}$

